## CS 2750 Machine Learning Lecture 13

## **Multilayer neural networks**

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**Backpropagation** Update weight  $w_{i,j}(k)$  using data D  $D = \{<\mathbf{x}, y>\}$   $w_{i,j}(k) \leftarrow w_{i,j}(k) - \alpha \frac{\partial}{\partial w_{i,j}(k)} J(D, \mathbf{w})$ Let  $\delta_i(k) = \frac{\partial}{\partial z_i(k)} J(D, \mathbf{w})$ Then:  $\frac{\partial}{\partial w_{i,j}(k)} J(D, \mathbf{w}) = \frac{\partial J(D, \mathbf{w})}{\partial z_i(k)} \frac{\partial z_i(k)}{\partial w_{i,j}(k)} = \delta_i(k) x_j(k-1)$ S.t.  $\delta_i(k)$  is computed from  $x_i(k)$  and the next layer  $\delta_i(k+1)$   $\delta_i(k) = \left[\sum_i \delta_i(k+1) w_{i,i}(k+1)\right] x_i(k)(1-x_i(k))$ Last unit (is the same as for the regular linear units):  $\delta_i(K) = -(y_u - f(\mathbf{x}_u, \mathbf{w}))$ It is the same for the classification with the log-likelihood measure of fit and linear regression with least-squares error!!!







































