

**CS 2750 Machine Learning  
Lecture 11**

**Evaluation of classifiers**

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**Classification model learning**

**Learning:**

- Many different ways and objective criteria used to learn the classification models. Examples:
  - Mean squared errors to learn the discriminant functions
  - Negative log likelihood (logistic regression)

**Evaluation:**

- One possibility: Use the same error criteria as used during the learning (apply to train & test data). Problems:
    - May work for discriminative models
    - Harder to interpret for humans.
  - **Question:** how to more naturally evaluate the classifier performance?
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## Evaluation of classification models

For any data set we use to test the classification model on we can build a **confusion matrix**:

- Counts of examples with:
- class label  $\omega_j$  that are classified with a label  $\alpha_i$

		target	
		$\omega = 1$	$\omega = 0$
predict	$\alpha = 1$	140	17
	$\alpha = 0$	20	54

## Evaluation of classification models

**Confusion matrix entries are often normalized with respect to the number of examples N to get proportions of the different agreements and disagreements among predicted and target values**

		target	
		$\omega = 1$	$\omega = 0$
predict	$\alpha = 1$	140 / 231	17 / 231
	$\alpha = 0$	20 / 231	54 / 231

## Basic evaluation statistics

Basic statistics calculated from the confusion matrix:

		target	
		$\omega = 1$	$\omega = 0$
predict	$\alpha = 1$	140	17
	$\alpha = 0$	20	54

**Classification Accuracy** =  $194/231$

## Basic evaluation statistics

Basic statistics calculated from the confusion matrix:

		target	
		$\omega = 1$	$\omega = 0$
predict	$\alpha = 1$	140	17
	$\alpha = 0$	20	54

**Classification Accuracy** =  $194/231$

**Misclassification Error** =  $37/231 = 1 - \text{Accuracy}$

## Evaluation for binary classification

Entries in the confusion matrix for binary classification have names:

		target	
		$\omega = 1$	$\omega = 0$
predict	$\alpha = 1$	<i>TP</i>	<i>FP</i>
	$\alpha = 0$	<i>FN</i>	<i>TN</i>

*TP*: True positive (hit)

*FP*: False positive (false alarm)

*TN*: True negative (correct rejection)

*FN*: False negative (a miss)

## Additional statistics

- Sensitivity (recall)

$$SENS = \frac{TP}{TP + FN}$$

- Specificity

$$SPEC = \frac{TN}{TN + FP}$$

- Positive predictive value (precision)

$$PPT = \frac{TP}{TP + FP}$$

- Negative predictive value

$$NPV = \frac{TN}{TN + FN}$$

## Binary classification: additional statistics

- Confusion matrix

		target		
		1	0	
predict	1	140	10	$PPV = 140/150$
	0	20	180	$NPV = 180/200$
		$SENS = 140/160$ $SPEC = 180/190$		

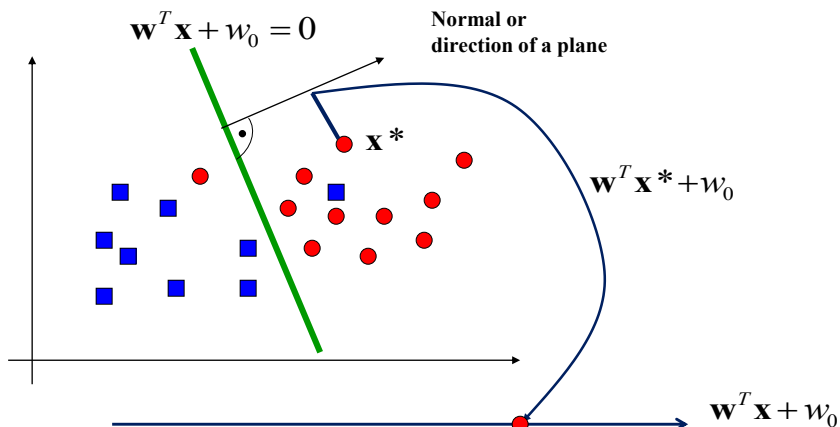
**Row and column quantities:**

- Sensitivity (SENS)
- Specificity (SPEC)
- Positive predictive value (PPV)
- Negative predictive value (NPV)

## Binary classification models

Often project data points to one dimensional space:

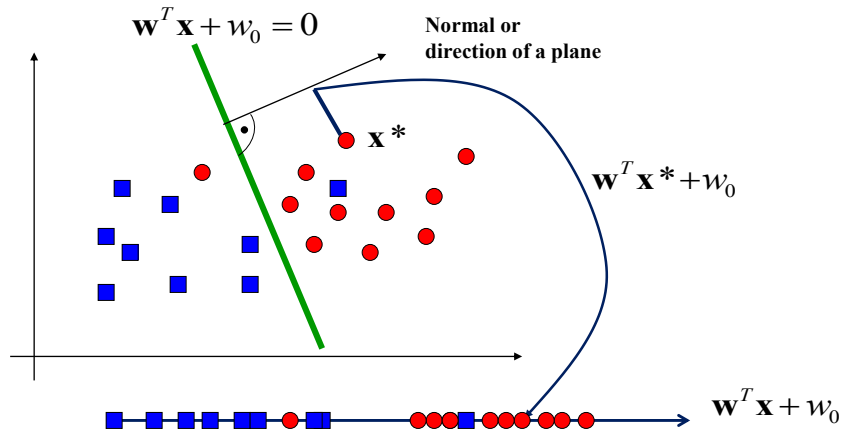
Defined for example by:  $w^T x + w_0$  or  $p(y=1|x,w)$



## Binary classification models

Often project data points to one dimensional space:

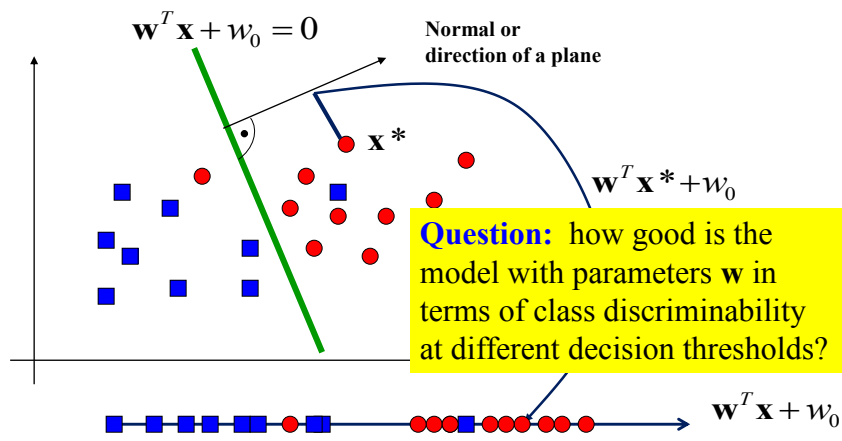
Defined for example by:  $\mathbf{w}^T \mathbf{x} + w_0$  or  $p(y=1|\mathbf{x}, \mathbf{w})$



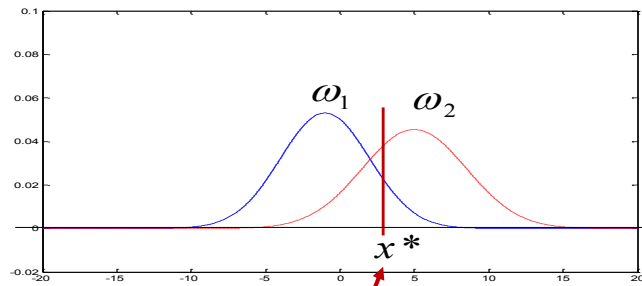
## Binary classification models

Often project data points to one dimensional space:

Defined for example by:  $\mathbf{w}^T \mathbf{x} + w_0$  or  $p(y=1|\mathbf{x}, \mathbf{w})$



## Receiver Operating Characteristic (ROC)



- **Probabilities:**

- *SENS*

- *SPEC*

threshold

$$p(x > x^* | \mathbf{x} \in \omega_2)$$

$$p(x < x^* | \mathbf{x} \in \omega_1)$$

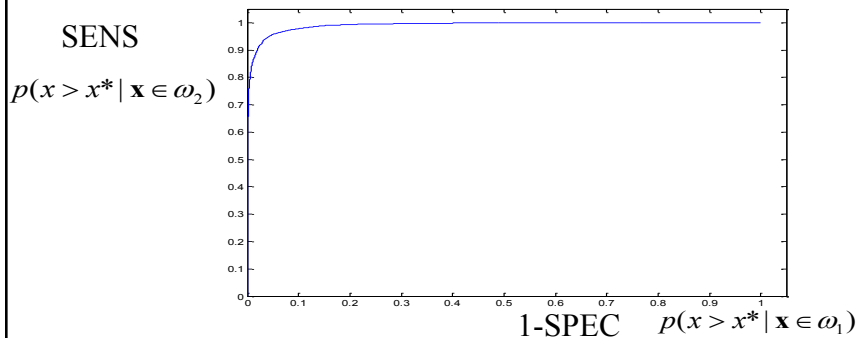
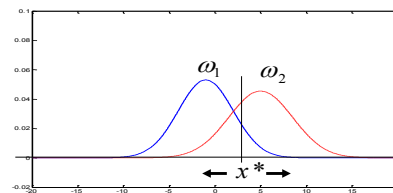
## Receiver Operating Characteristic (ROC)

- **ROC curve plots :**

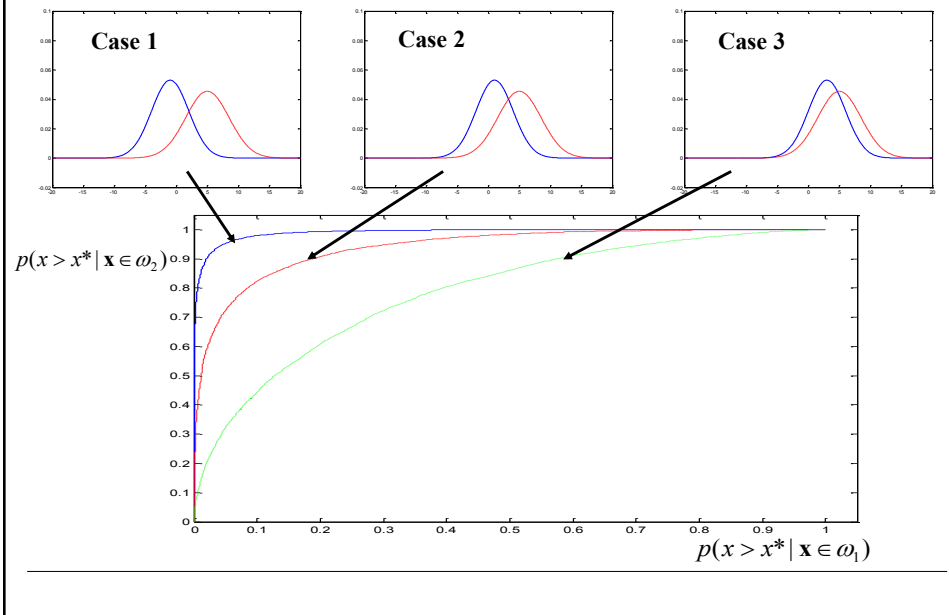
$$SN = p(x > x^* | \mathbf{x} \in \omega_2)$$

$$1-SP = p(x > x^* | \mathbf{x} \in \omega_1)$$

for different  $x^*$



## ROC curve



## Receiver operating characteristic

- **ROC**
  - shows the discriminability between the two classes under different thresholds representing different decision biases
- **Decision bias**
  - can be changed using the different loss function
- **Quality of a classification model:**
  - Area under the ROC
  - Best value 1, worst (no discriminability): 0.5