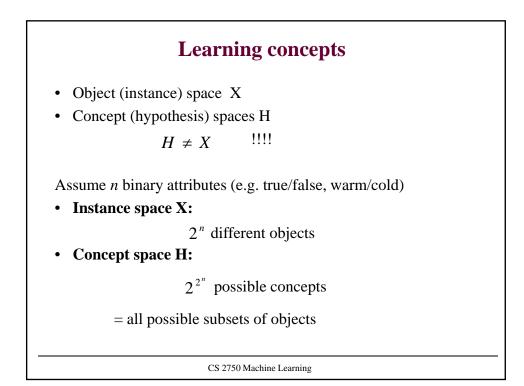


Most general and most specific consistent hypothesis. Aitchell's version space algorithm Probably approximately correct (PAC) learning.	tline:	
Aitchell's version space algorithm Probably approximately correct (PAC) learning. Sample complexity for PAC. Vapnik-Chervonenkis (VC) dimension.	Learning boolean functions	
Probably approximately correct (PAC) learning. Sample complexity for PAC. /apnik-Chervonenkis (VC) dimension.	Most general and most specified	fic consistent hypothesis.
Sample complexity for PAC. Vapnik-Chervonenkis (VC) dimension.	Mitchell's version space algo	orithm
/apnik-Chervonenkis (VC) dimension.	Probably approximately corr	ect (PAC) learning.
	Sample complexity for PAC.	
mproved sample complexity bounds.	Vapnik-Chervonenkis (VC)	limension.
	improved sample complexity	bounds.

			•		4			
Learning concepts								
Acour	no objecto	(aromnla	a) dasar	ribad in	torma	attributas		
Assui	ne objects	s (example	s) uesci	illeu ill		auributes.		
Sky	Air-Temp	Humidity	Wind	Water	Forecast	EnjoySport		
Sunny	Warm	Normal	Strong	Warm	Same	yes		
Rainy	Cold	Normal	Strong	Warm	Change	no		
	•	t of objec	ts					
• Co	ncept lea	rning:						
	-					earn a boolean		
ma	pping from	n objects	to T/F i	dentifyi	ng an und	lerlying concep		
_	E.g. Enjo	ySport con	acept					
• Co	ncept (hyj	pothesis) s	pace H					
_	Restrictio	on on the b	oolean	descript	tion of cor	ncepts		
	1 1	on on the b	1	descript	tion of con	ncepts		

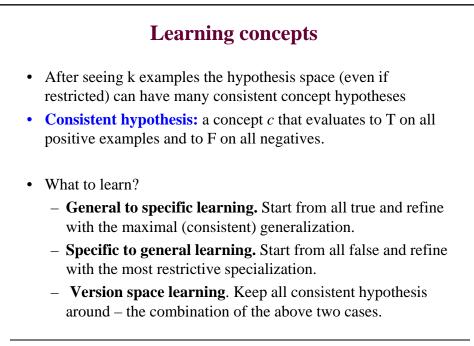


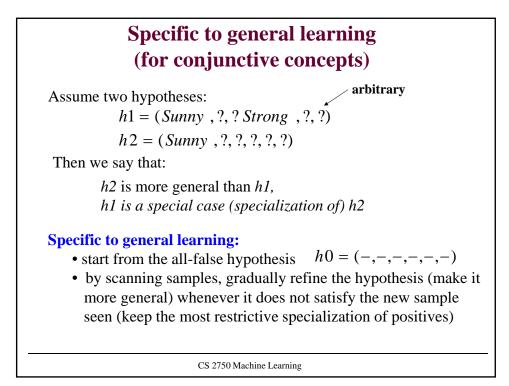
Learning concepts
Problem: Concept space too large
Solution: restricted hypothesis space H
Example: conjunctive concepts

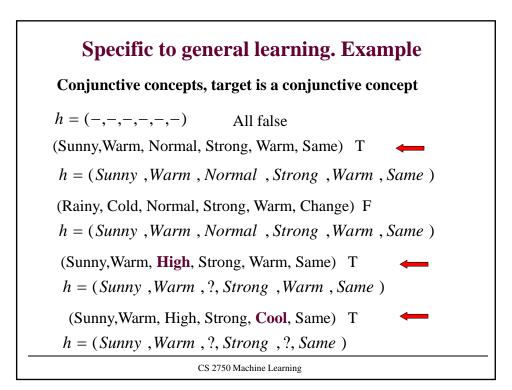
(Sky = Sunny) ∧ (Weather = Cold)
3ⁿ possible concepts

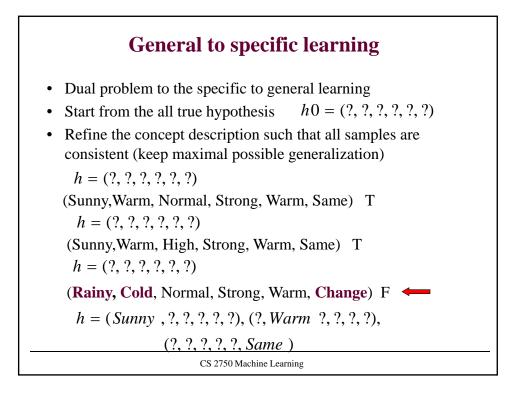
Other restricted spaces:

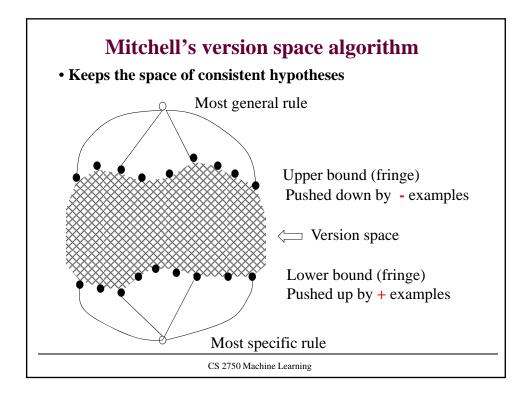
3-CNF (or k-CNF)
(a₁ × a₃ × a₇) ∧ (...)
3-DNF (or k-DNF)
(a₁ × a₅ × a₉) ∨ (...)

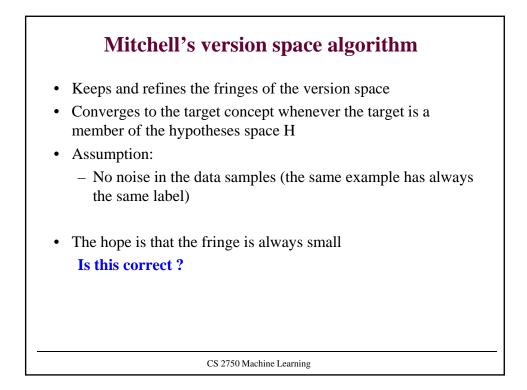


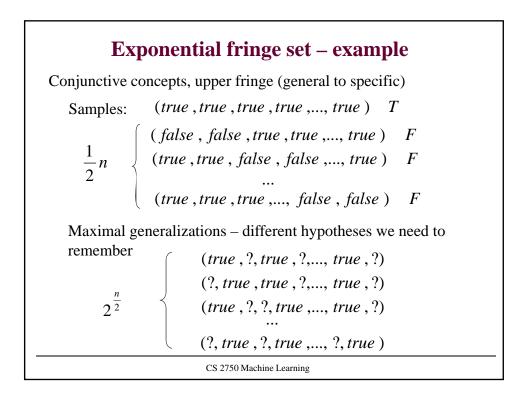


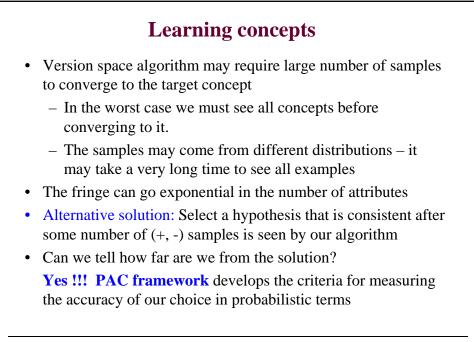


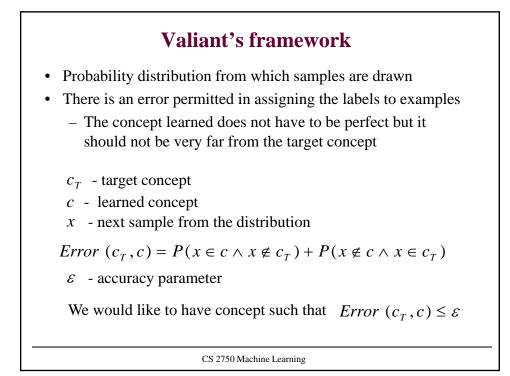


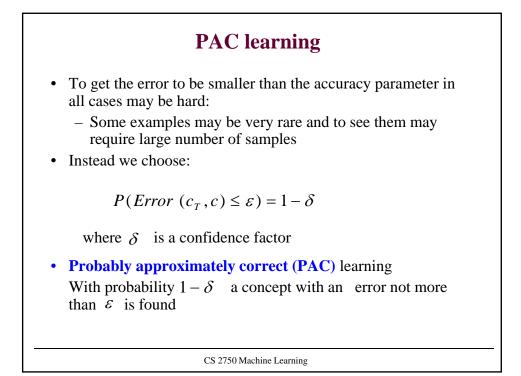


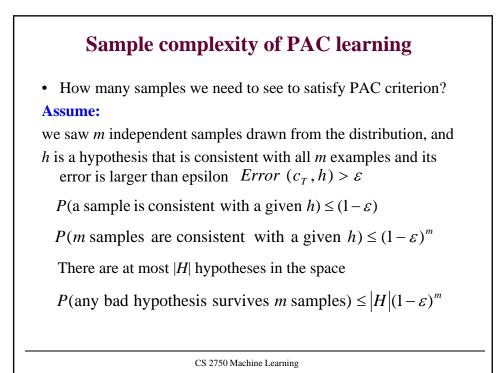












Sample complexity of PAC learning

 $P(\text{any bad hypothesis survives } m \text{ samples}) \leq |H|(1-\varepsilon)^m$

 $\leq |H|e^{-\varepsilon m}$

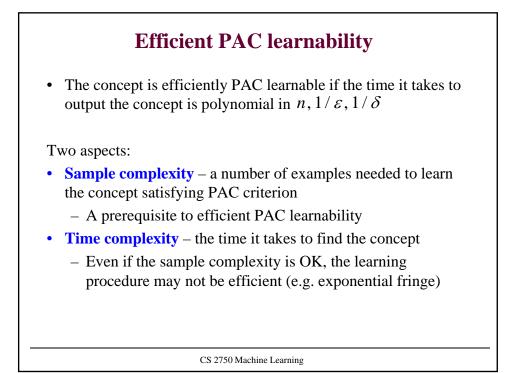
In the PAC framework we want to bound this probability with the confidence factor δ

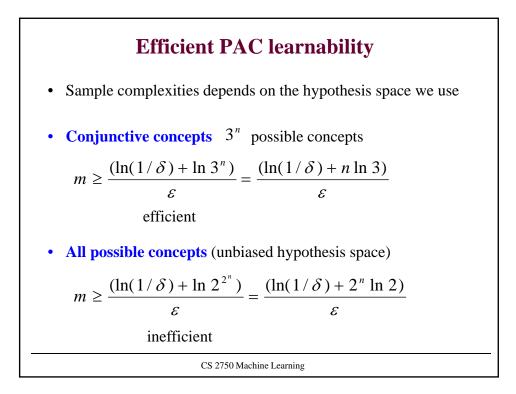
$$|H|e^{-\varepsilon m} \leq \delta$$

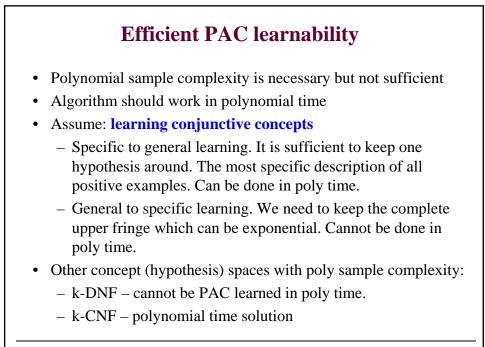
Expressing for m

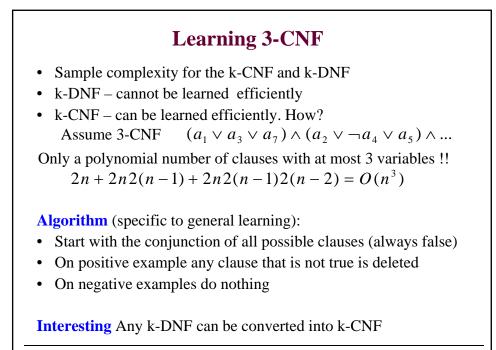
$$m \geq \frac{(\ln(1/\delta) + \ln|H|)}{\varepsilon}$$

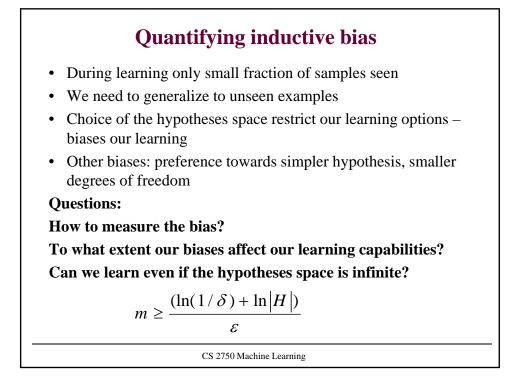
After *m* samples satisfying the above inequality any consistent hypothesis satisfies the PAC criterion

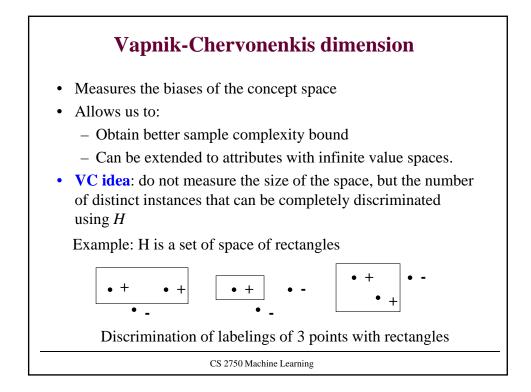


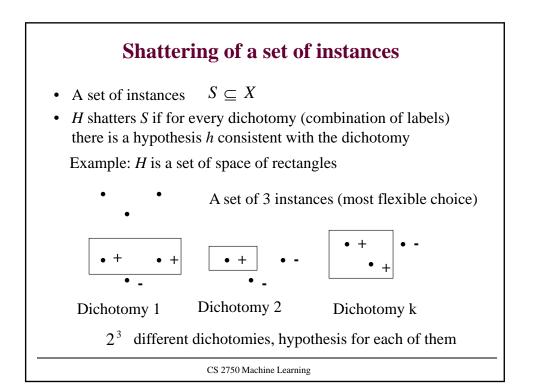


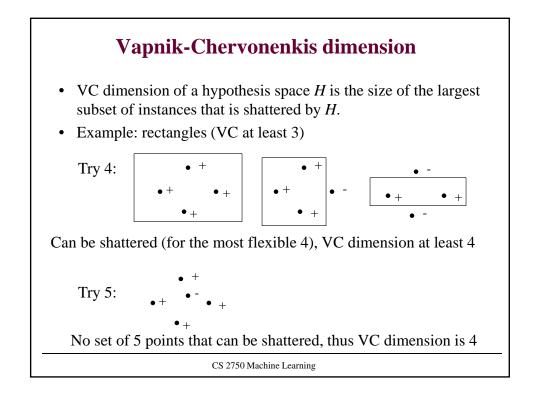


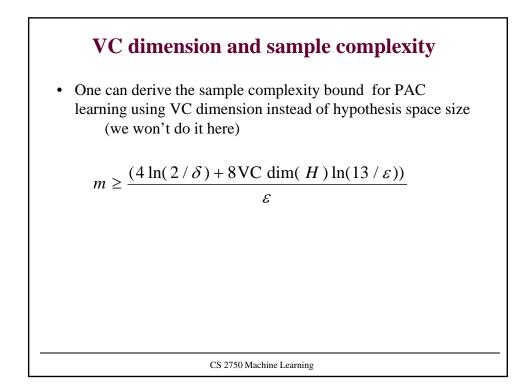












Adding noise

- We have a target concept but there is a chance of mislabeling the examples seen
- Can we PAC-learn also in this case?
- Blumer (1986). If h is a hypothesis that agrees with at least

$$m = \frac{1}{\varepsilon} \ln(\frac{n}{\delta})$$

samples drawn from the distribution then

$$P(error(h, c_{\tau}) \geq \varepsilon) \leq \delta$$

Mitchell gives the sample complexity bound for the choice of the hypothesis with the best training error

CS 2750 Machine Learning

