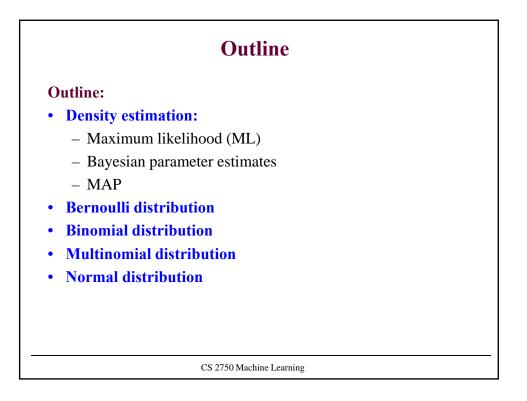
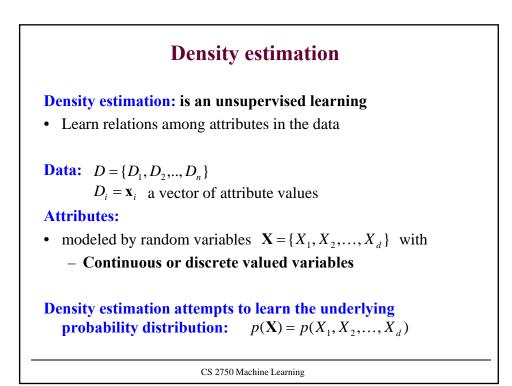
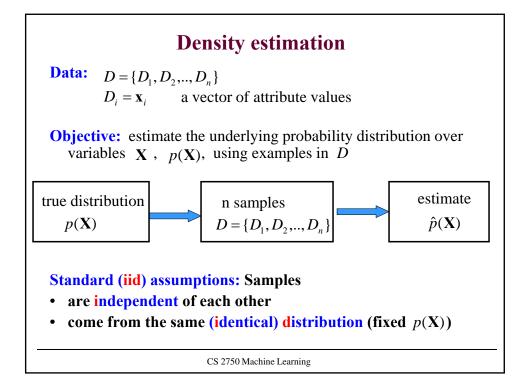
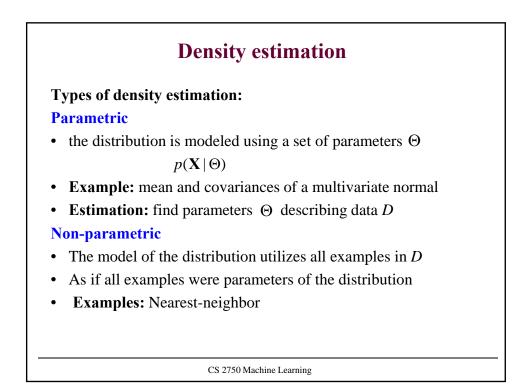


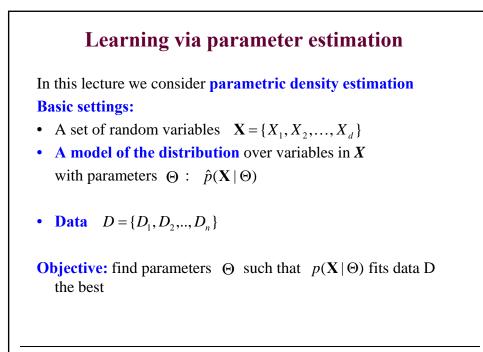
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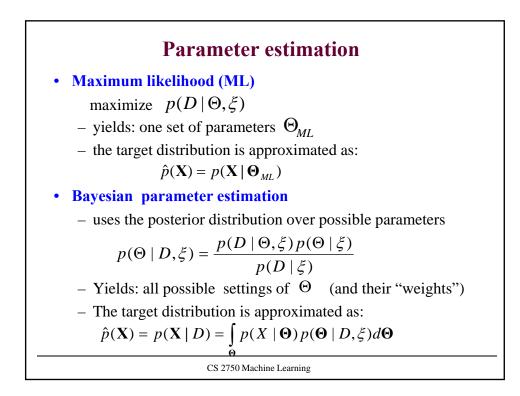


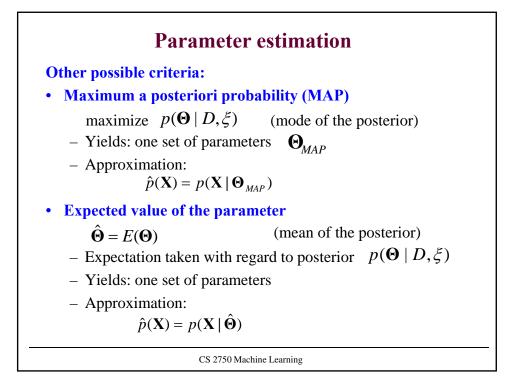


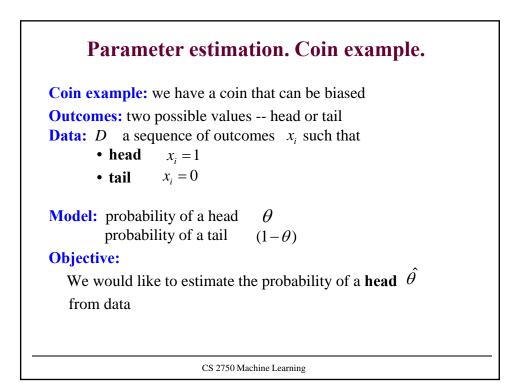


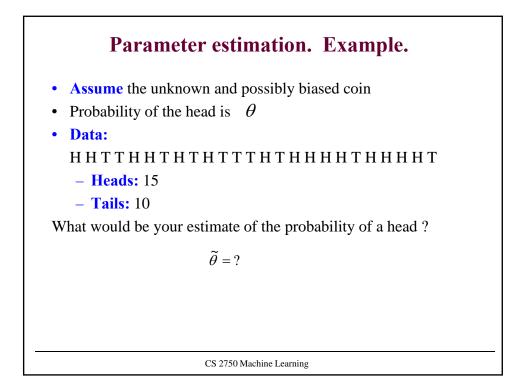


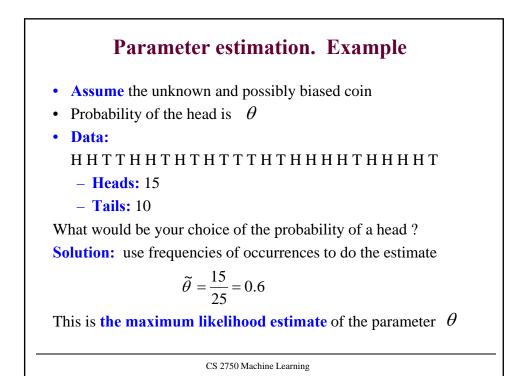
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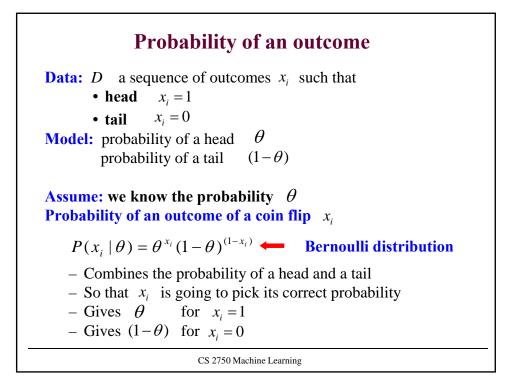


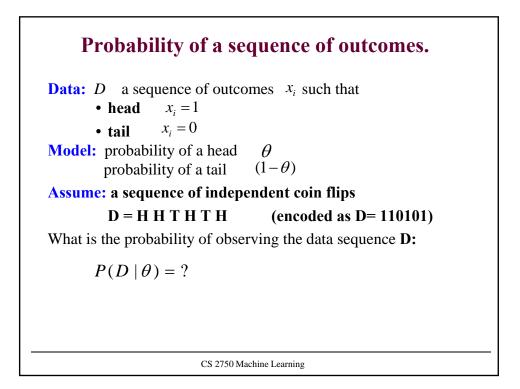


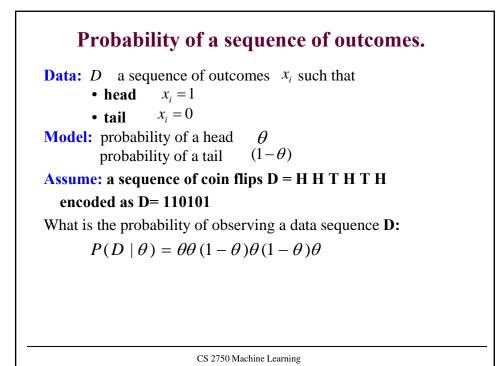


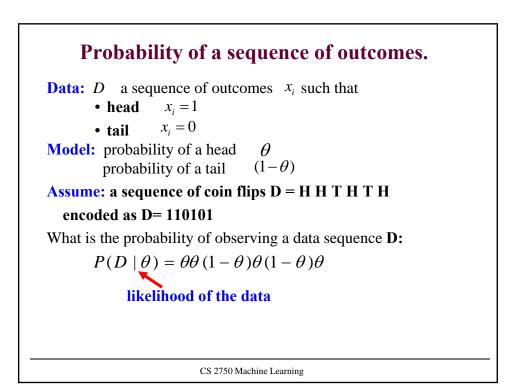


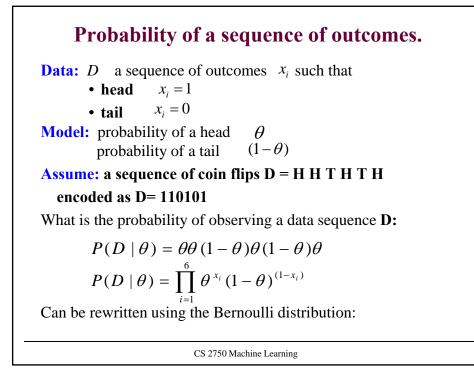






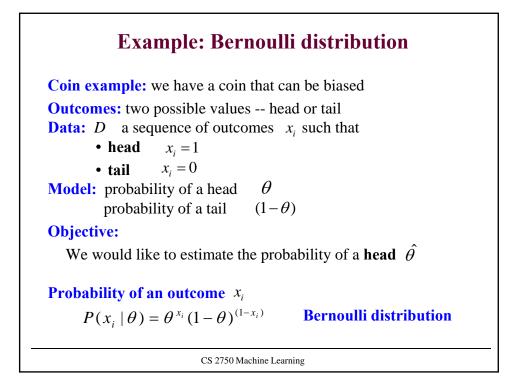


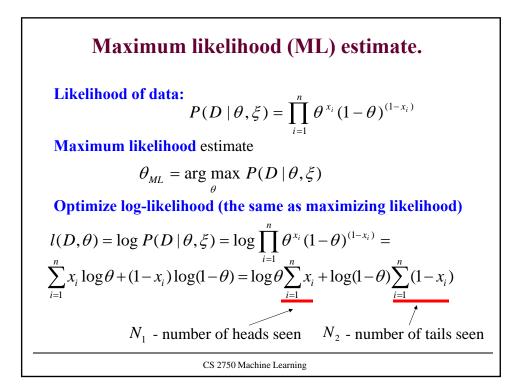


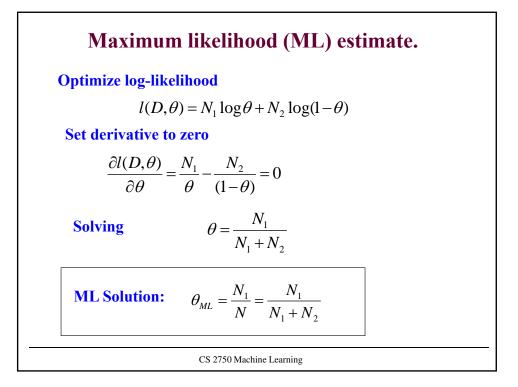


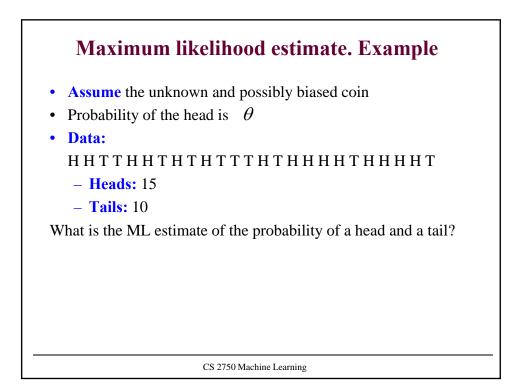
## **The goodness of fit to the data** Learning: we do not know the value of the parameter $\theta$ Our learning goal: • Find the parameter $\theta$ that fits the data D the best? **One solution to the "best":** Maximize the likelihood $P(D | \theta) = \prod_{i=1}^{n} \theta^{x_i} (1-\theta)^{(1-x_i)}$ **Intuition:** • more likely are the data given the model, the better is the fit Note: Instead of an error function that measures how bad the data fit the model we have a measure that tells us how well the data fit : $Error(D, \theta) = -P(D | \theta)$

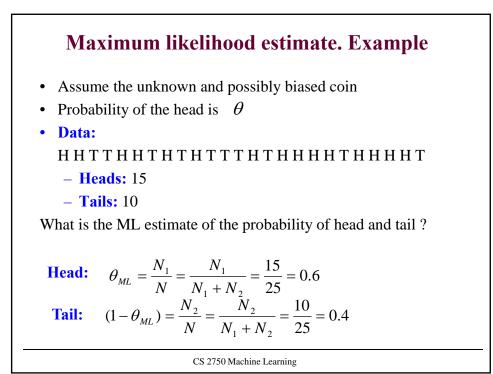
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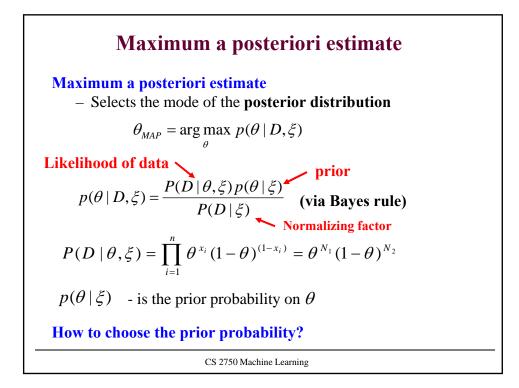












## **Prior distribution**

**Choice of prior: Beta distribution** 

$$p(\theta \mid \xi) = Beta(\theta \mid \alpha_1, \alpha_2) = \frac{\Gamma(\alpha_1 + \alpha_2)}{\Gamma(\alpha_1)\Gamma(\alpha_2)} \theta^{\alpha_1 - 1} (1 - \theta)^{\alpha_2 - 1}$$

 $\Gamma(x)$  - a Gamma function  $\Gamma(x) = (x-1)\Gamma(x-1)$ For integer values of x  $\Gamma(n) = (n-1)!$ 

Why to use Beta distribution? Beta distribution "fits" Bernoulli trials - conjugate choices

$$P(D \mid \theta, \xi) = \theta^{N_1} (1 - \theta)^{N_2}$$

Posterior distribution is again a Beta distribution

$$p(\theta \mid D, \xi) = \frac{P(D \mid \theta, \xi)Beta(\theta \mid \alpha_1, \alpha_2)}{P(D \mid \xi)} = Beta(\theta \mid \alpha_1 + N_1, \alpha_2 + N_2)$$
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