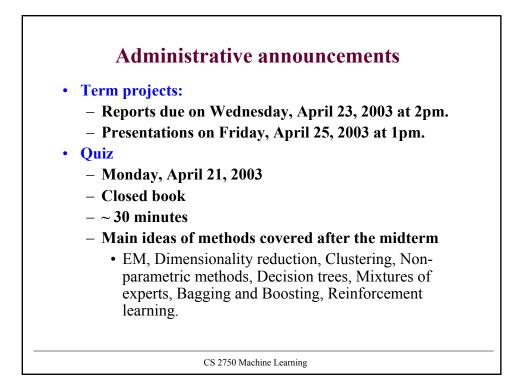
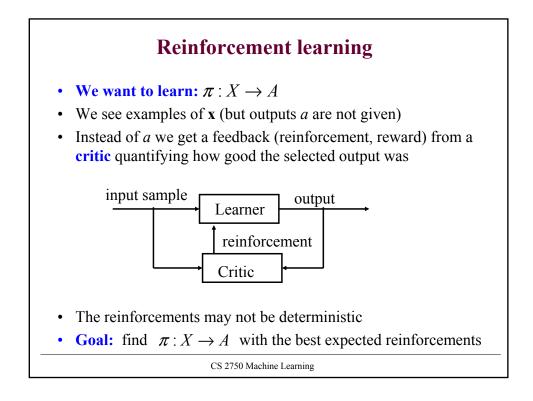
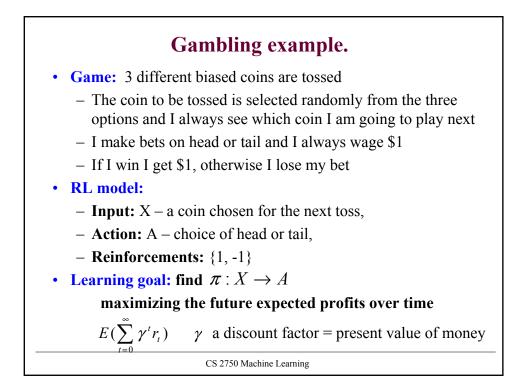
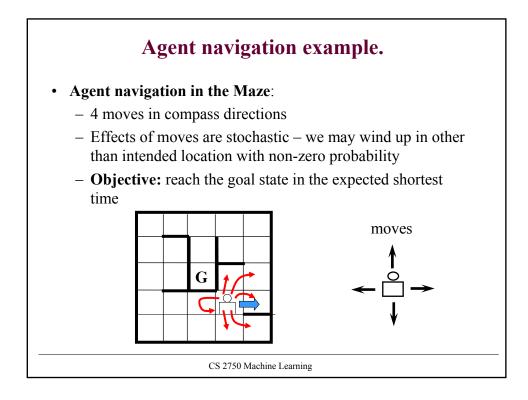
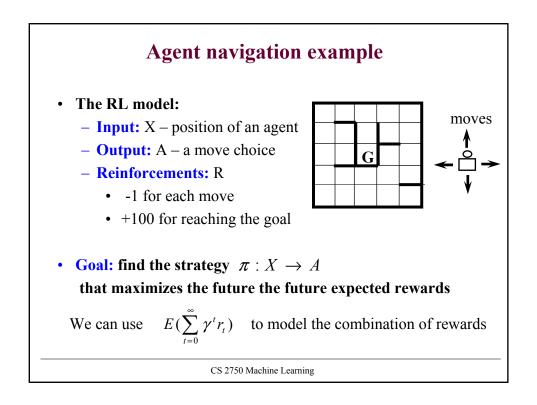
CS 2750 Machine Learning Lecture 22 Reinforcement learning Milos Hauskrecht <u>milos@cs.pitt.edu</u> 5329 Sennott Square

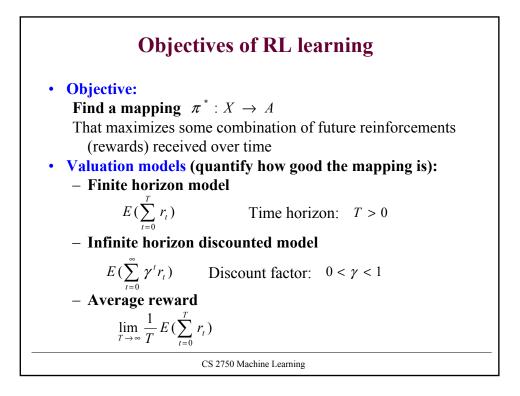


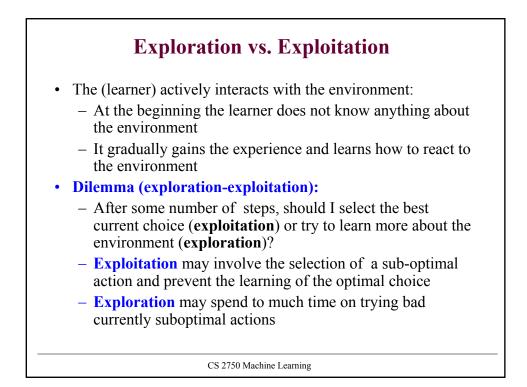




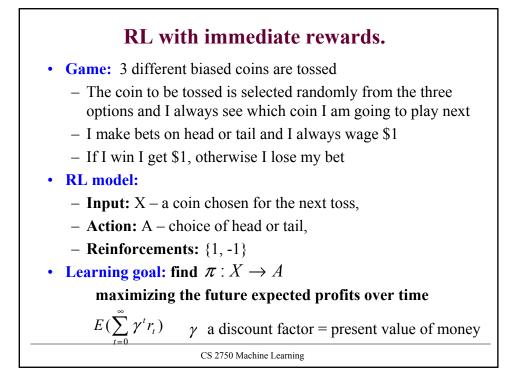








Effects of actions on the environment (next input x to be seen) No effect, the distribution over possible x is fixed; action consequences (rewards) are seen immediately, Otherwise, distribution of x can change; the rewards related to the action can be seen with some delay. Leads to two forms of reinforcement learning: Learning with immediate rewards Gambling example Learning with delayed rewards Agent navigation example; move choices affect the state of the environment (position changes), a big reward at the goal state is delayed



RL with immediate rewards

• Expected reward

 $E(\sum_{t=0}^{\infty} \gamma^t r_t) \quad \gamma$ - A discount factor = present value of money

- Immediate reward case:
 - Reward for the choice becomes available immediately
 - Our choice does not affect environment

$$E\left(\sum_{t=0}^{n} \gamma^{t} r_{t}\right) = E\left(r_{0}\right) + E\left(\gamma r_{1}\right) + E\left(\gamma^{2} r_{2}\right) + \dots$$

 r_0 , r_1 , r_2 ... Rewards for every step

- Expected reward for input x and the choice a in one step: $R(\mathbf{x}, a)$

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RL with immediate rewards

Immediate reward case:

- Reward for the choice *a* becomes available immediately
- Expected reward for the input x and choice a: R(x, a)
 - For the gambling problem it can be defined as:

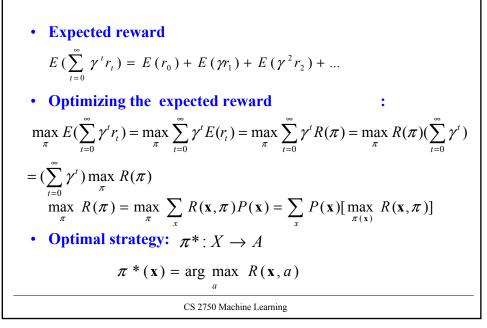
$$R(\mathbf{x}, a_i) = \sum_j r(a_i \mid \boldsymbol{\omega}_j, \mathbf{x}) P(\boldsymbol{\omega}_j \mid \mathbf{x})$$

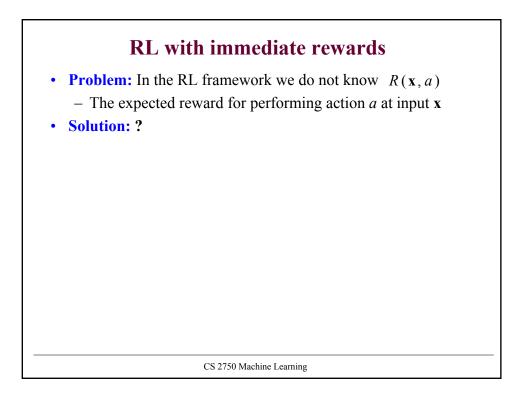
- $-\omega_{j}$ a "hidden" outcome of the coin toss
- Recall the definition of the expected loss
- Expected one step reward for a strategy $\pi: X \to A$

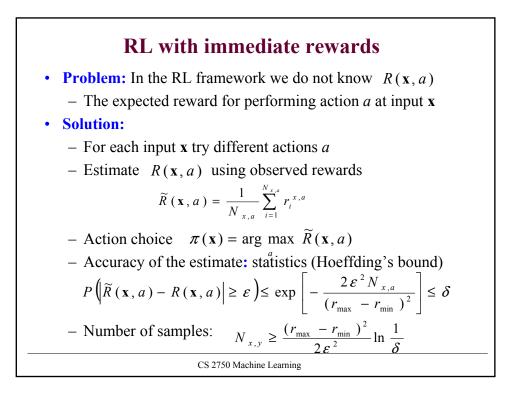
$$R(\boldsymbol{\pi}) = \sum_{\mathbf{x}} R(\mathbf{x}, \boldsymbol{\pi}(\mathbf{x})) P(\mathbf{x})$$

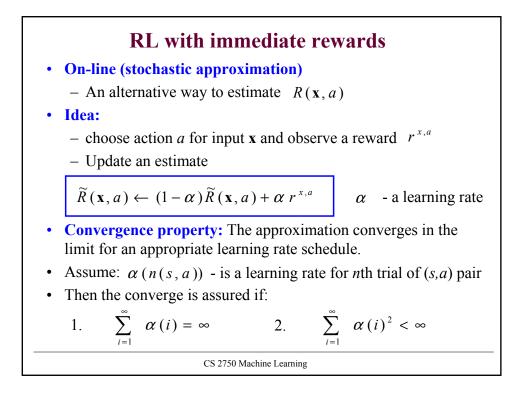
 $R(\pi)$ is the expected reward for $r_0, r_1, r_2 \dots$

RL with immediate rewards



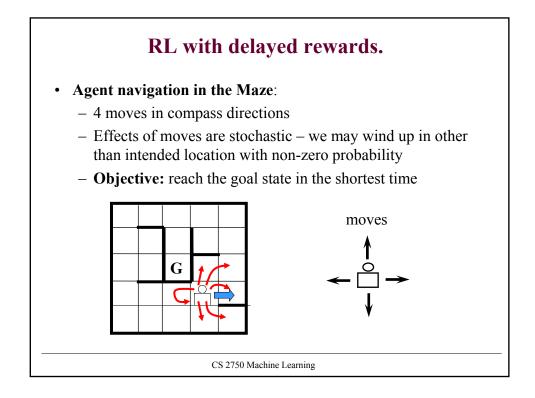


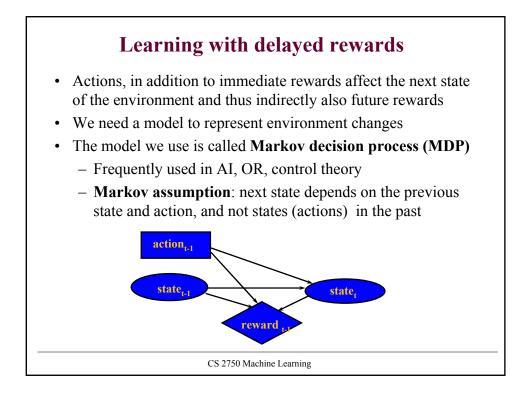


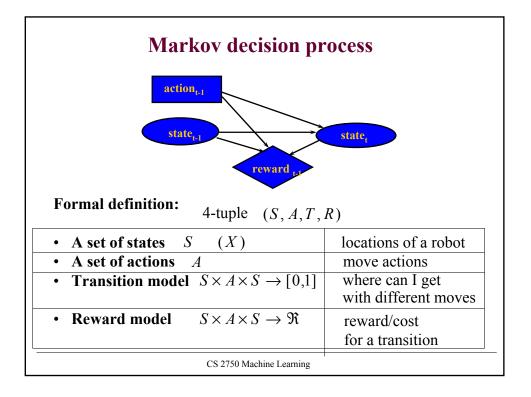


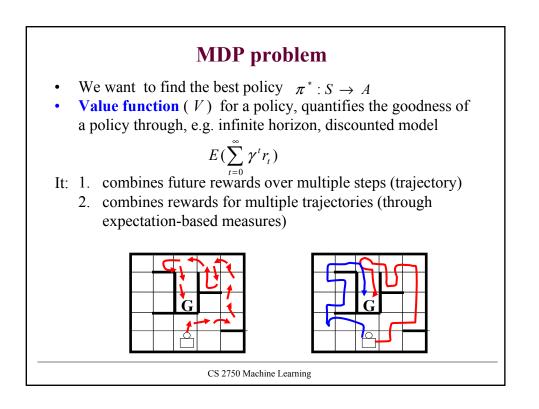
Exploration vs. Exploitation In the RL framework the (learner) actively interacts with the environment. At any point in time it has an estimate of *R̃*(**x**, *a*) for any input action pair Dilemma: Should the learner use the current best choice of action (exploitation) *π̂*(**x**) = arg max *R̃*(**x**, *a*) Or choose other action *a* and further improve its estimate (exploration) Different exploration/exploitation strategies exist

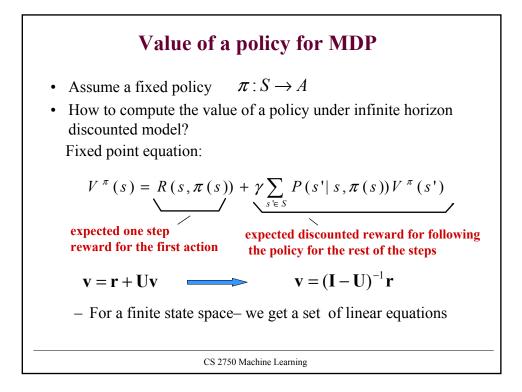
Exploration vs. Exploitation
Uniform exploration
– Choose the "current" best choice with probability $1 - \varepsilon$
$\hat{\pi}(\mathbf{x}) = \arg \max \widetilde{R}(\mathbf{x}, a)$
- All other choices are selected with a uniform probability ε
$\frac{\mathcal{E}}{\mid A \mid -1}$
Boltzman exploration
– The action is chosen randomly but proportionally to its
current expected reward estimate
$p(a \mid \mathbf{x}) = \frac{\exp\left[\widetilde{R}(x, a) / T\right]}{\sum_{a' \in A} \exp\left[\widetilde{R}(x, a') / T\right]}$
T – is temperature parameter
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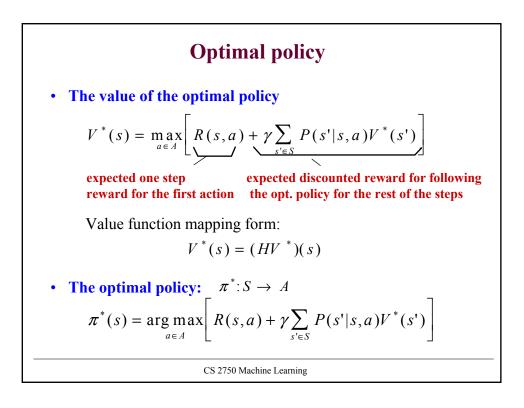


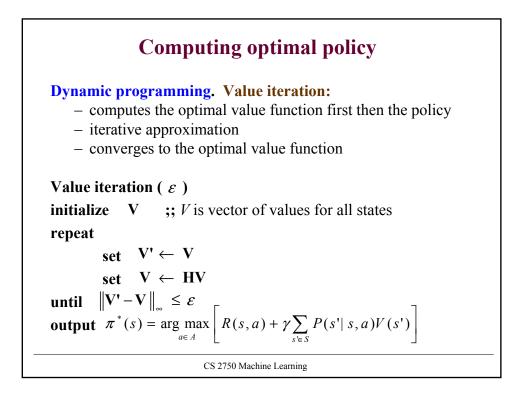


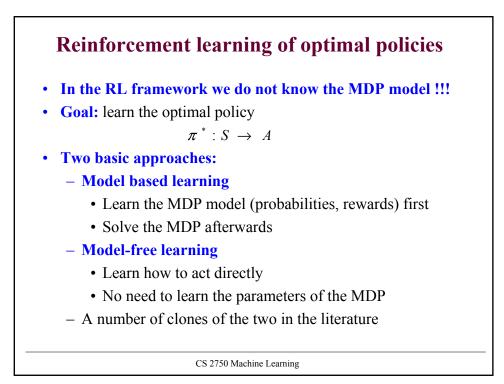


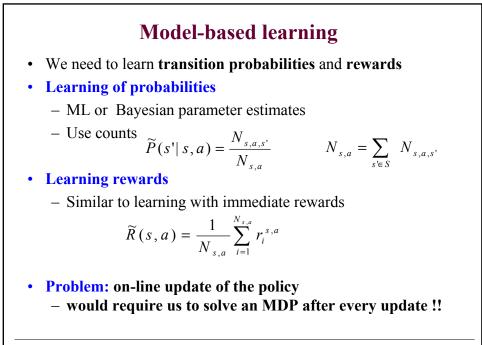






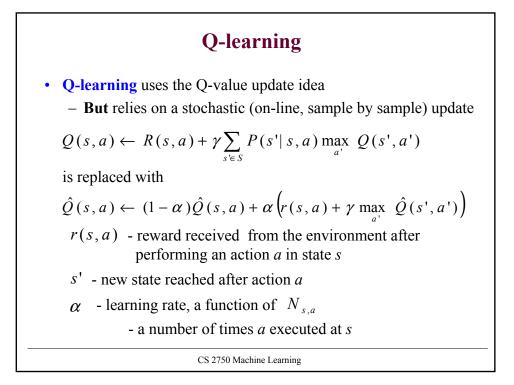


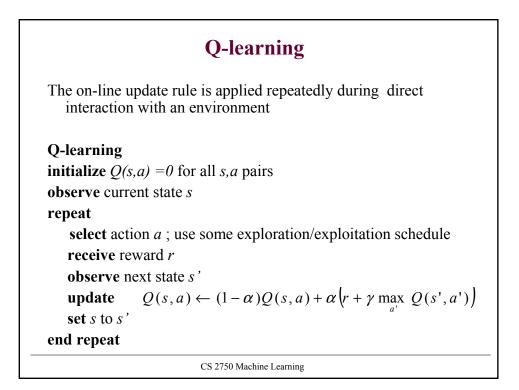


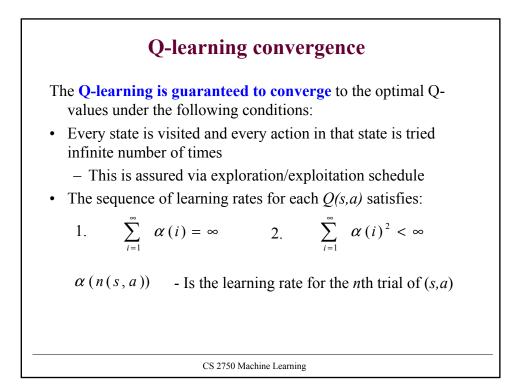


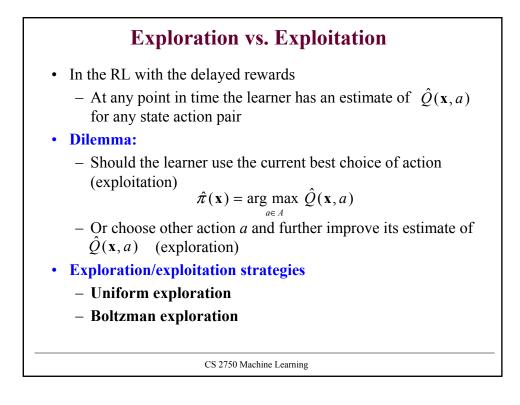
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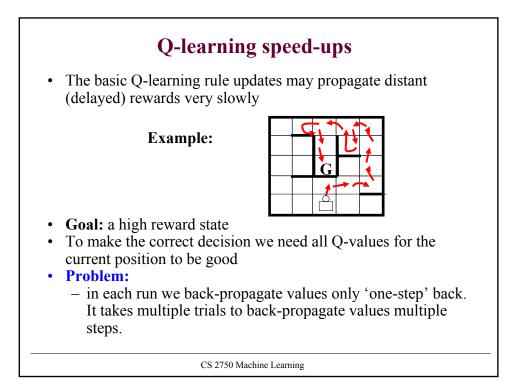
Model free learning • Motivation: value function update (value iteration): $V(s) \leftarrow \max_{a \in A} \left[R(s, a) + \gamma \sum_{s' \in S} P(s' | s, a) V(s') \right]$ • Let $Q(s, a) = R(s, a) + \gamma \sum_{s' \in S} P(s' | s, a) V(s')$ • Then $V(s) \leftarrow \max_{a \in A} Q(s, a)$ • Note that the update can be defined purely in terms of Q-functions $Q(s, a) \leftarrow R(s, a) + \gamma \sum_{s' \in S} P(s' | s, a) \max_{a'} Q(s', a')$ CS 2750 Machine Learning

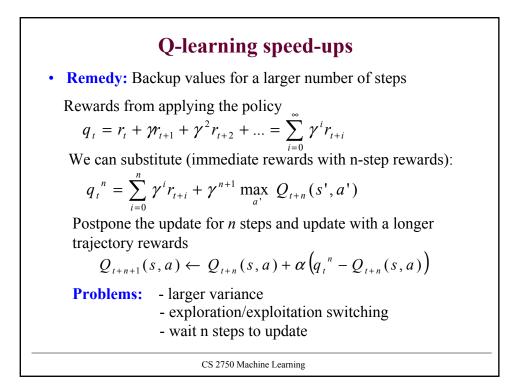


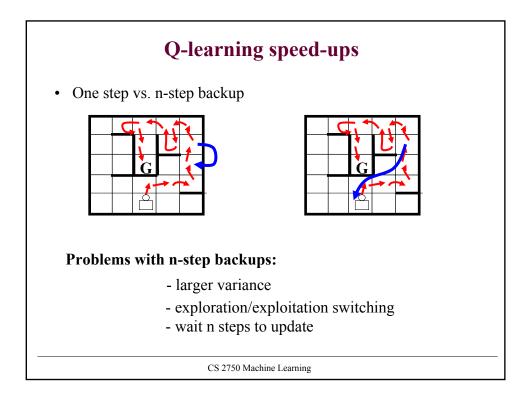


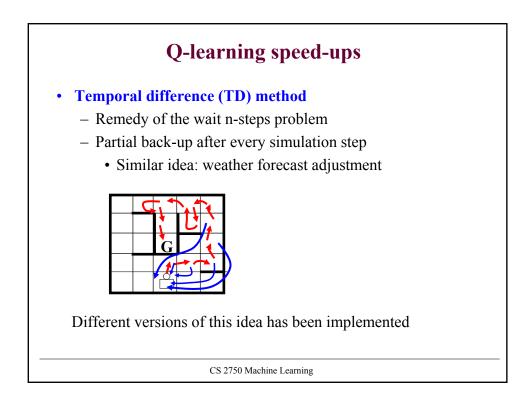












RL successes

- Reinforcement learning is relatively simple
 - On-line techniques can track non-stationary environments and adapt to its changes

• Successful applications:

- TD Gammon learned to play backgammon on the championship level
- Elevator control
- Dynamic channel allocation in mobile telephony
- Robot navigation in the environment