CS 2750 Machine Learning Lecture 13

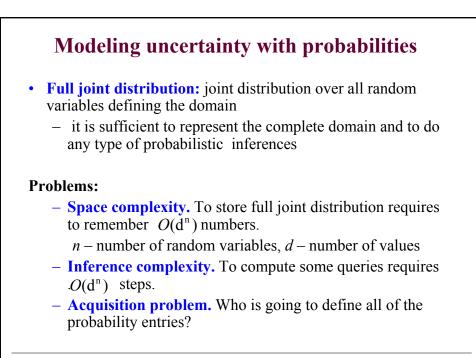
Bayesian belief networks. Inference.

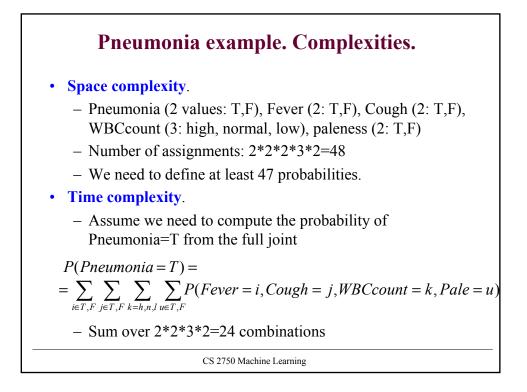
Milos Hauskrecht <u>milos@cs.pitt.edu</u> 5329 Sennott Square

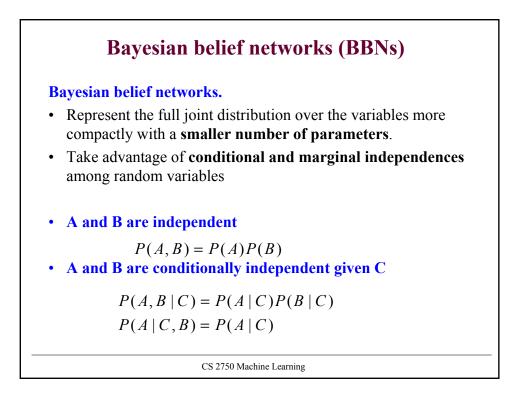
CS 2750 Machine Learning

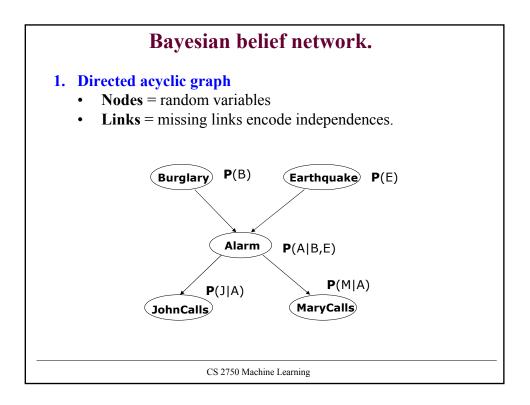
Monday, March 17, 2003 • In class • Closed book • Material covered by Wednesday, March 12 • Last year midterm will be posted on the web

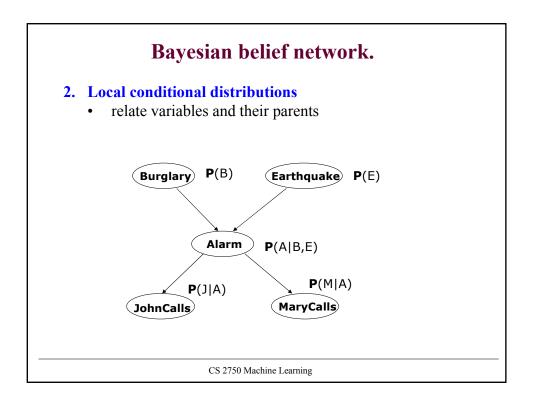
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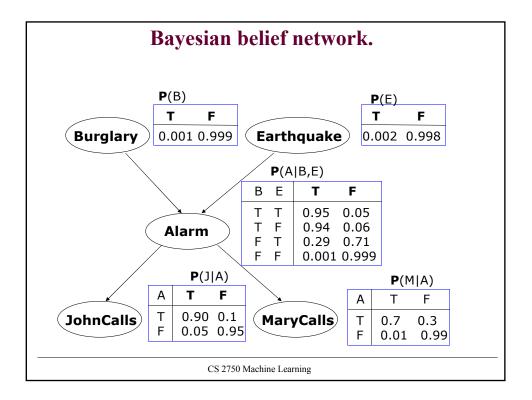


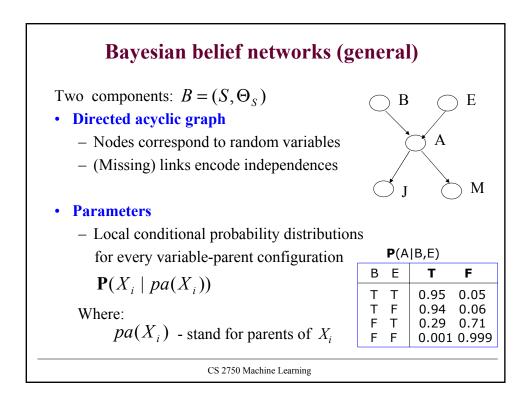


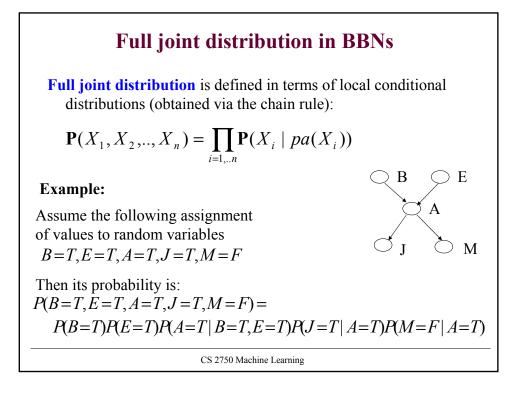


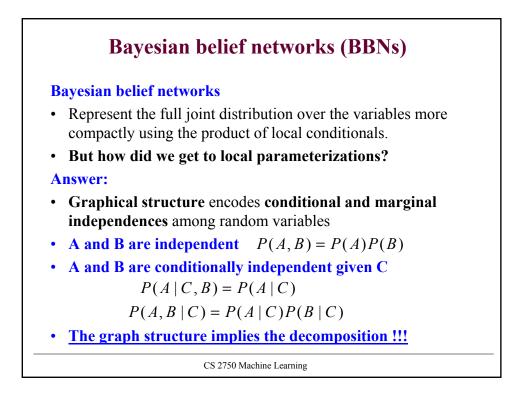


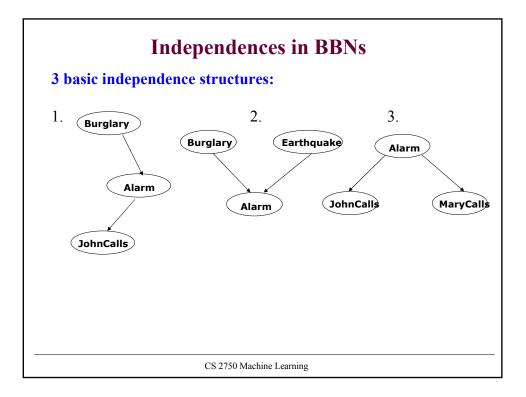


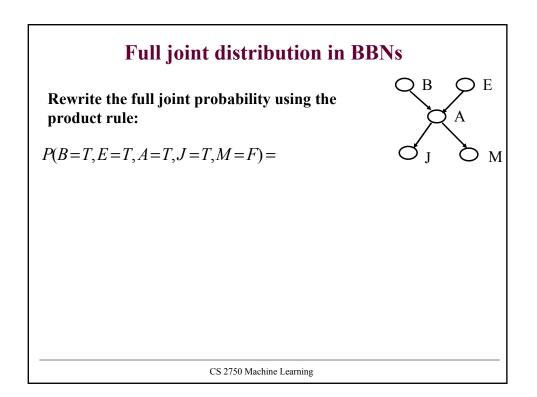


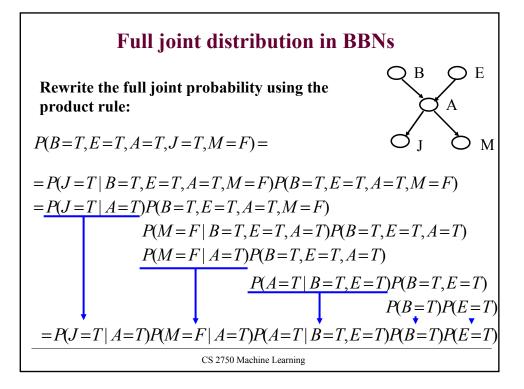


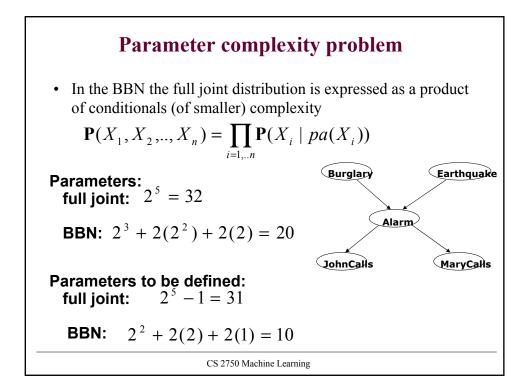


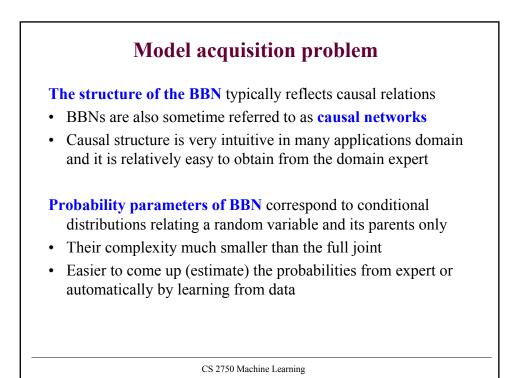


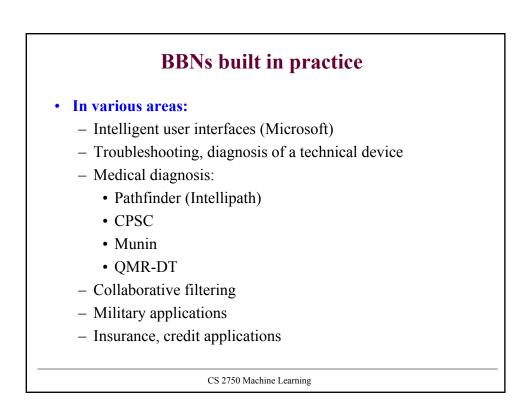


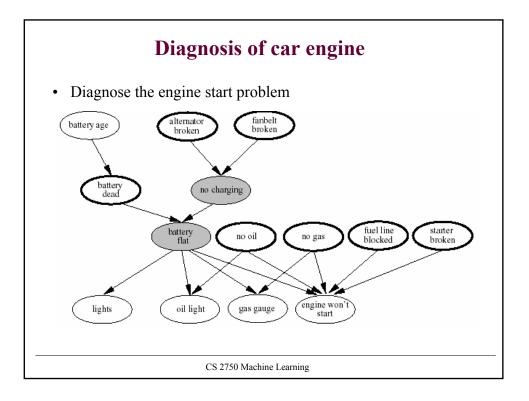


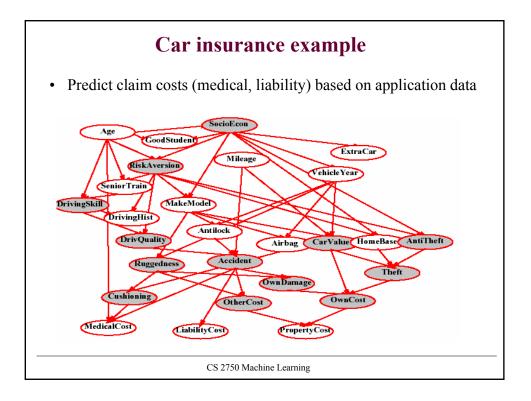


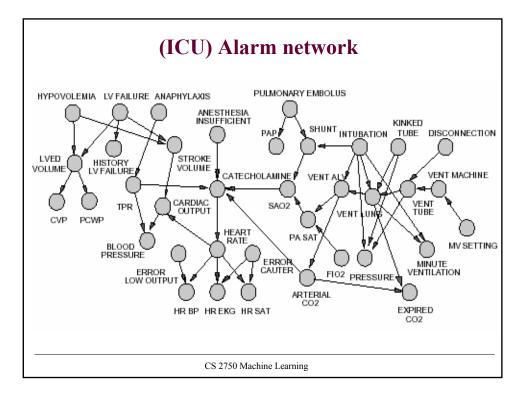


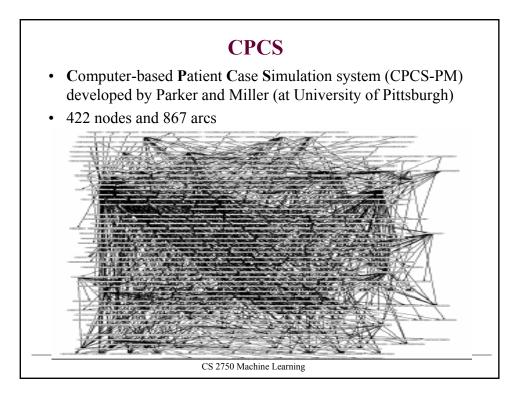


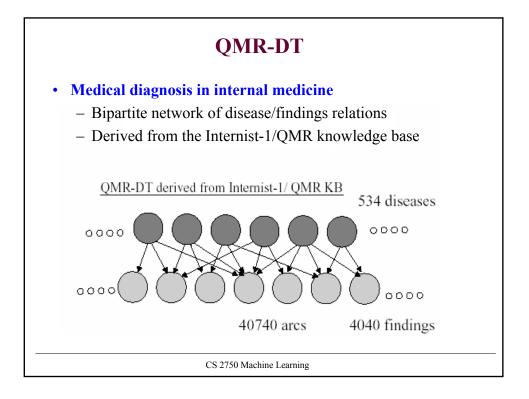


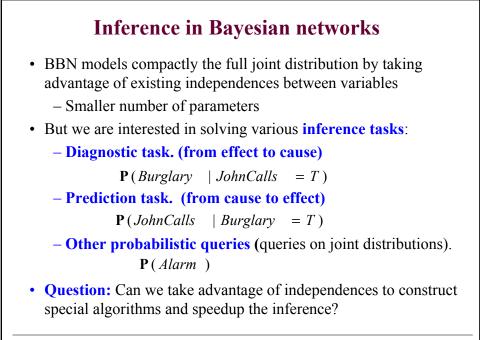


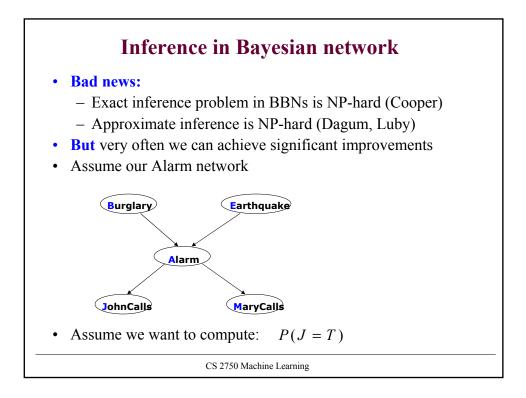




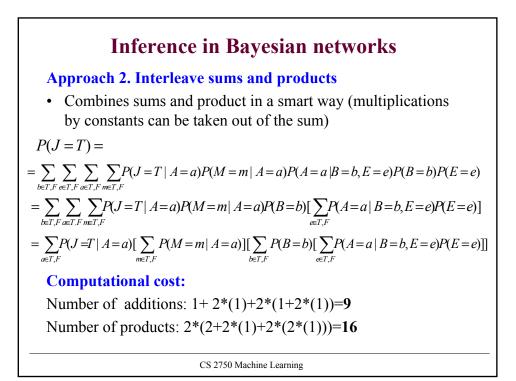


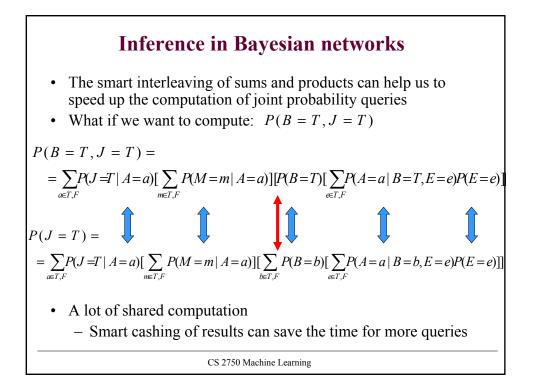


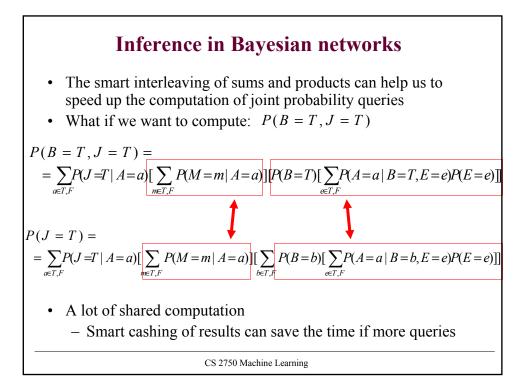




Inference in Bayesian networks Computing: P(J = T) **Approach 1. Blind approach.** • Sum out all un-instantiated variables from the full joint, • express the joint distribution as a product of conditionals P(J = T) = $= \sum_{b \in T, F} \sum_{a \in T, F} \sum_{m \in T, F} P(B = b, E = e, A = a, J = T, M = m)$ $= \sum_{b \in T, F} \sum_{a \in T, F} \sum_{m \in T, F} P(J = T | A = a)P(M = m | A = a)P(A = a | B = b, E = e)P(B = b)P(E = e)$ **Computational cost:** Number of additions: **15** Number of products: 16*4=**64**







Inference in Bayesian networks• When cashing of results becomes handy?• What if we want to compute a diagnostic query: $P(B = T | J = T) = \frac{P(B = T, J = T)}{P(J = T)}$ • Exactly probabilities we have just compared !!• There are other queries when cashing and ordering of sums and products can be shared and saves computation $P(B | J = T) = \frac{P(B, J = T)}{P(J = T)} = \alpha P(B, J = T)$ • General technique: Variable elimination

