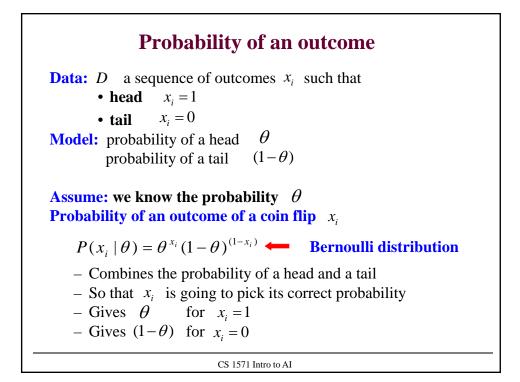
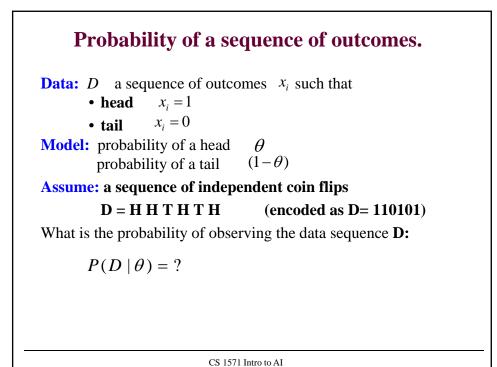


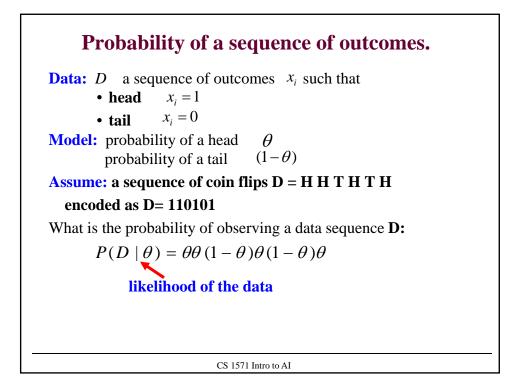
This is the maximum likelihood estimate of the parameter θ

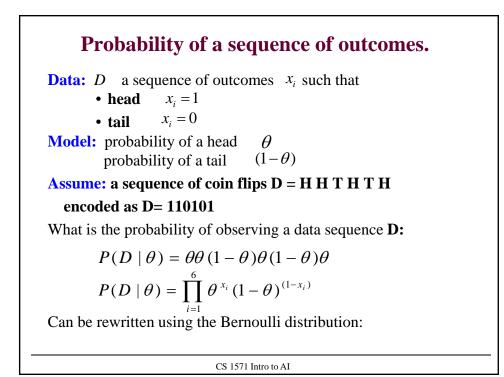
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Determine the equation of th





The goodness of fit to the data.

Learning: we do not know the value of the parameter θ Our learning goal:

• Find the parameter θ that fits the data D the best? One solution to the "best": Maximize the likelihood

$$P(D \mid \theta) = \prod_{i=1}^{n} \theta^{x_i} (1-\theta)^{(1-x_i)}$$

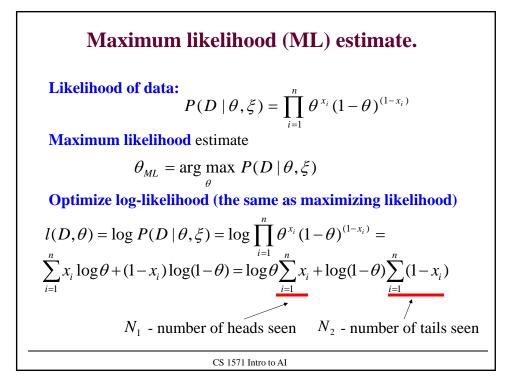
Intuition:

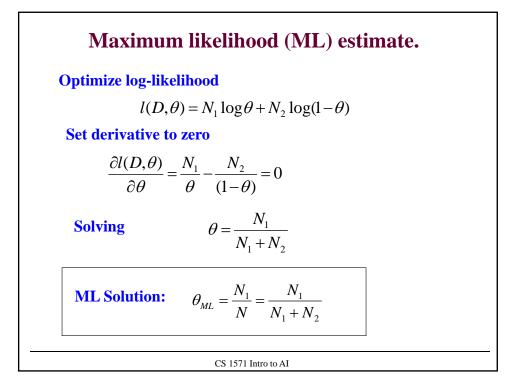
• more likely are the data given the model, the better is the fit

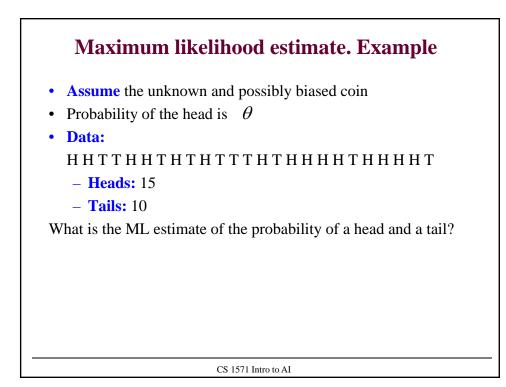
Note: Instead of an error function that measures how bad the data fit the model we have a measure that tells us how well the data fit :

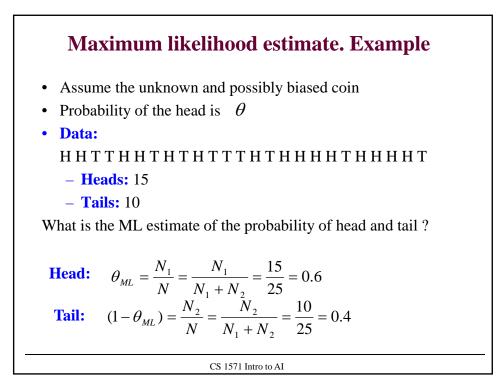
Error $(D, \theta) = -P(D \mid \theta)$

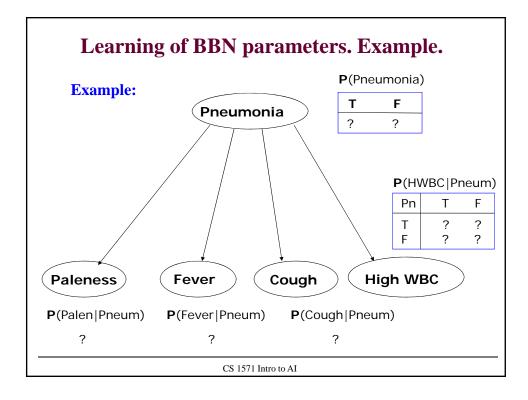
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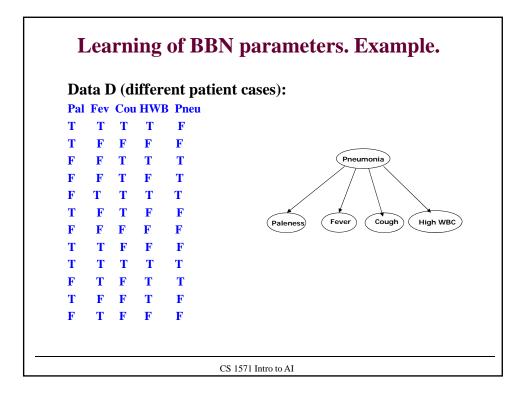


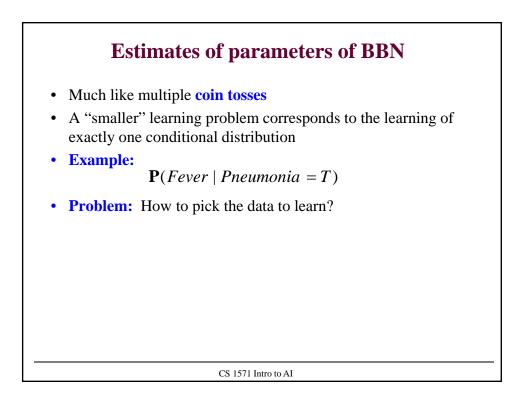


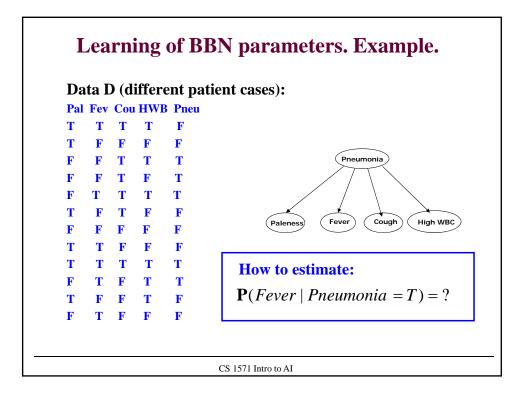


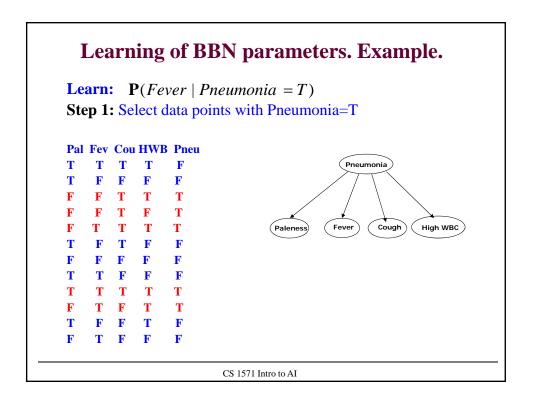


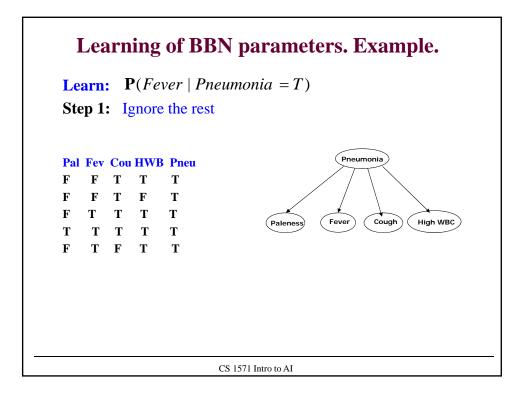


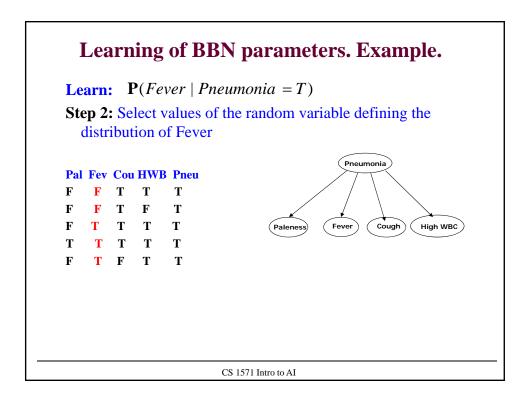


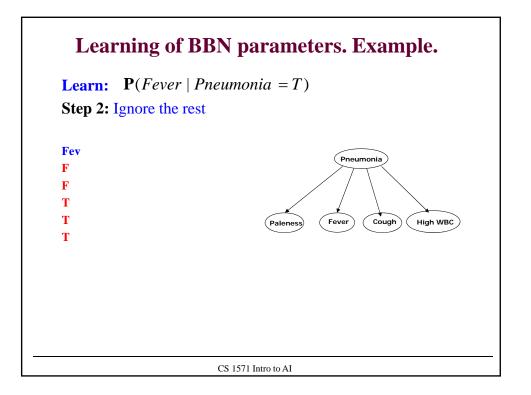


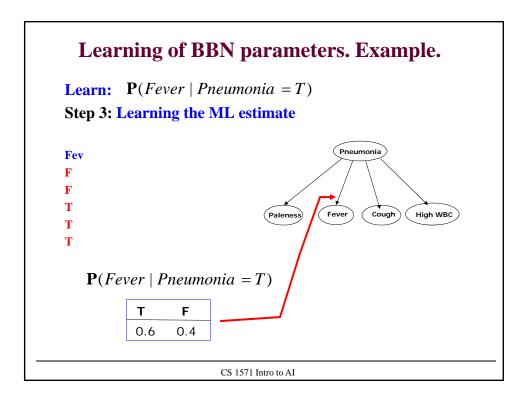










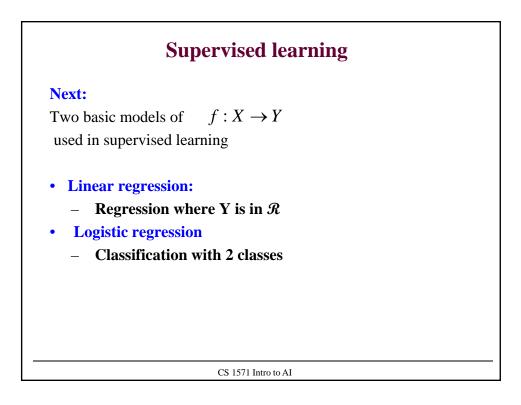


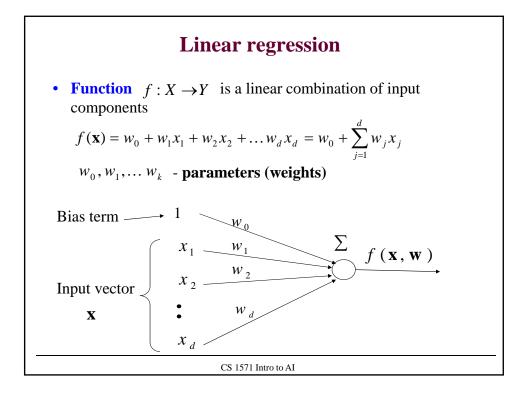
Supervised learning

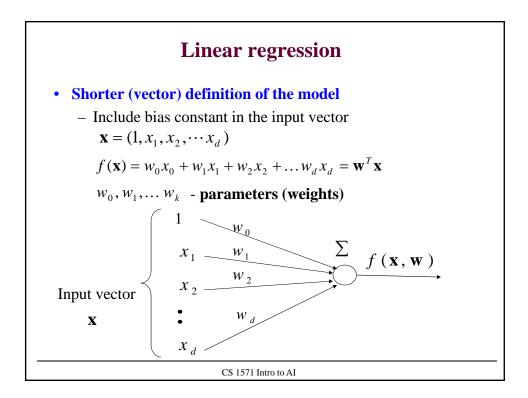
Data: D = {D₁, D₂,...,D_n} a set of *n* examples D_i =< x_i, y_i > x_i = (x_{i,1}, x_{i,2}, ..., x_{i,d}) is an input vector of size d y_i is the desired output (given by a teacher)
Objective: learn the mapping f : X → Y s.t. y_i ≈ f(x_i) for all i = 1,..., n
Regression: Y is continuous Example: earnings, product orders → company stock price

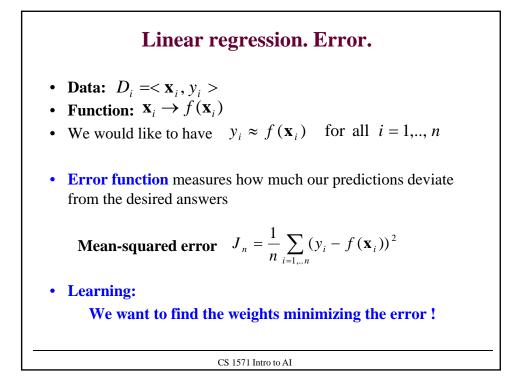
• Classification: Y is discrete Example: handwritten digit in binary form → digit label

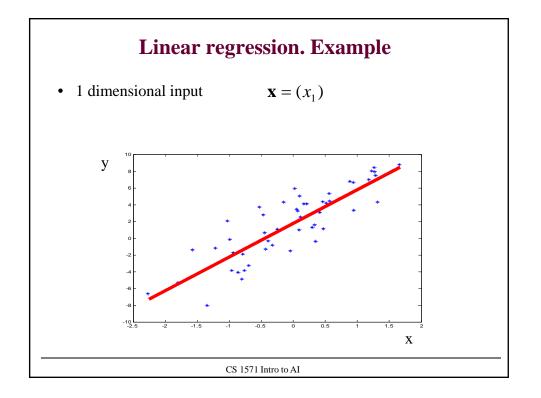
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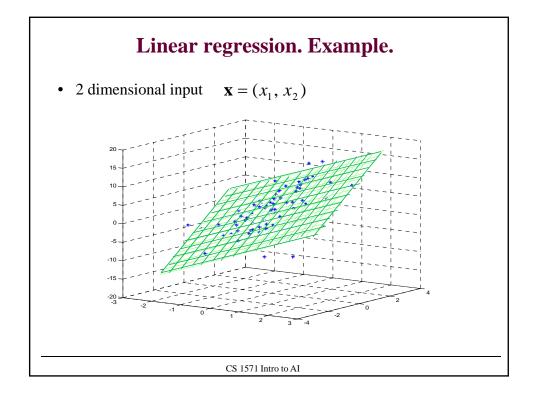












Linear regression. Optimization. • We want the weights minimizing the error $J_n = \frac{1}{n} \sum_{i=1,..n} (y_i - f(\mathbf{x}_i))^2 = \frac{1}{n} \sum_{i=1,..n} (y_i - \mathbf{w}^T \mathbf{x}_i)^2$ • For the optimal set of parameters, derivatives of the error with respect to each parameter must be 0 $\frac{\partial}{\partial w_j} J_n(\mathbf{w}) = -\frac{2}{n} \sum_{i=1}^n (y_i - w_0 x_{i,0} - w_1 x_{i,1} - ... - w_d x_{i,d}) x_{i,j} = 0$ • Vector of derivatives: $grad_{\mathbf{w}} (J_n(\mathbf{w})) = \nabla_{\mathbf{w}} (J_n(\mathbf{w})) = -\frac{2}{n} \sum_{i=1}^n (y_i - \mathbf{w}^T \mathbf{x}_i) \mathbf{x}_i = \overline{\mathbf{0}}$

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