

Conjunctive Normal Form

$$\forall x (P(x) \rightarrow (\forall y (P(y) \rightarrow P(f(x,y))) \wedge \neg \forall y (Q(x,y) \rightarrow P(y))))$$

2. Eliminate \rightarrow

$$\forall x (\neg P(x) \vee (\forall y (\neg P(y) \vee P(f(x,y))) \wedge \neg \forall y (\neg Q(x,y) \vee P(y))))$$

3. Reduce scope of negation

$$\forall x (\neg P(x) \vee (\forall y (\neg P(y) \vee P(f(x,y))) \wedge \exists y (Q(x,y) \wedge \neg P(y))))$$

4. Standardize variables

$$\forall x (\neg P(x) \vee (\forall y (\neg P(y) \vee P(f(x,y))) \wedge \exists z (Q(x,z) \wedge \neg P(z))))$$

5. Eliminate existential quantification (skolemize)

$$\forall x (\neg P(x) \vee (\forall y (\neg P(y) \vee P(f(x,y))) \wedge (Q(x,g(x)) \wedge \neg P(g(x)))))$$

6. Drop universal quantification symbols

$$(\neg P(x) \vee ((\neg P(y) \vee P(f(x,y))) \wedge (Q(x,g(x)) \wedge \neg P(g(x)))))$$

7. Convert to conjunction of disjunctions (distribute)

$$(\neg P(x) \vee (\neg P(y) \vee P(f(x,y)))) \wedge (\neg P(x) \vee (Q(x,g(x)) \wedge \neg P(g(x)))) \\ (\neg P(x) \vee \neg P(y) \vee P(f(x,y))) \wedge (\neg P(x) \vee Q(x,g(x))) \wedge (\neg P(x) \vee \neg P(g(x)))$$

1. all X (read (X) --> literate (X))
 2. all X (dolphin (X) --> ~literate (X))
 3. exists X (dolphin (X) ^ intelligent (X))
- (a translation of "Some dolphins are intelligent")

"Are there some who are intelligent but cannot read?"

4. exists X (intelligent(X) ^ ~read (X))

Set of clauses (1-3):

1. ~read(X) v literate(X)
2. ~dolphin(Y) v ~literate(Y)
- 3a. dolphin (a)
- 3b. intelligent (a)

Negation of 4:

$$\sim(\text{exists } Z (\text{intelligent}(Z) \wedge \sim\text{read} (Z)))$$

In Clausal form:

$$\sim\text{intelligent}(Z) \vee \text{read}(Z)$$

Resolution proof (on board)