### CS 2740 Knowledge representation Lecture 23

# Decision making in the presence of uncertainty II

Milos Hauskrecht <u>milos@cs.pitt.edu</u> 5329 Sennott Square



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Oil wildcatter problem				
• Assume that in addition to the drill/no-drill choices we have an option to run the seismic resonance test				
Seismic resonance test results:				
- Closed pattern (more likely when the hole holds the oil)				
- <b>Diffuse pattern</b> (more likely when empty)				
$\mathbf{P}(Oil \mid Seismic \ resonance \ test)$				
Seismic resonance test pattern				
		closed	diffuse	
Oil	True	0.8	0.2	
	False	0.3	0.7	
• Test cost: 10K				
CS 2750 Machine Learning				













### Value of information

- When the test makes sense?
- Only when its result makes the decision maker to change his mind, that is he decides not to drill.
- Value of information:
  - Measure of the goodness of the information from the test
  - Difference between the expected value with and without the test information
- Oil wildcatter example:
  - Expected value without the test = 18
  - Expected value with the test = 25.4
  - Value of information for the seismic test = 7.4











### Axioms of the utility theory

• **Orderability:** Given any two states, the a rational agent prefers one of them, else the two as equally preferable.

$$(A \succ B) \lor (B \succ A) \lor (A \sim B)$$

• **Transitivity:** Given any three states, if an agent prefers *A* to *B* and prefers *B* to C, agent must prefer *A* to C.

 $(A \succ B) \land (B \succ C) \Longrightarrow (A \succ C)$ 

• **Continuity:** If some state *B* is between *A* and C in preference, then there is a *p* for which the rational agent will be indifferent between state B and the lottery in which A comes with probability p, C with probability (1-p).

$$(A \succ B \succ C) \Longrightarrow \exists p [p : A; (1-p) : C] \sim B$$



## **Utility theory**

If the agent obeys the axioms of the utility theory, then

1. there exists a real valued function U such that:

 $U(A) > U(B) \Leftrightarrow A \succ B$  $U(A) = U(B) \Leftrightarrow A \sim B$ 

2. The utility of the lottery is the expected utility, that is the sum of utilities of outcomes weighted by their probability

U[p:A;(1-p):B] = pU(A) + (1-p)U(B)

3. Rational agent makes the decisions in the presence of uncertainty by maximizing its expected utility









