# Part-of- <br> Speech Tagging 

## Chapter 8

(8.1-8.4.6)

## Outline

- Parts of speech (POS)
- Tagsets
- POS Tagging
- Rule-based tagging
- Probabilistic (HMM) tagging


## Garden Path Sentences

- The old dog the footsteps of the young


## Parts of Speech

- Traditional parts of speech
- Noun, verb, adjective, preposition, adverb, article, interjection, pronoun, conjunction, etc
- Called: parts-of-speech, lexical categories, word classes, morphological classes, lexical tags...
- Lots of debate within linguistics about the number, nature, and universality of these
- We'll completely ignore this debate.


## Parts of Speech

- Traditional parts of speech
- ~ 8 of them



## POS examples

- N noun chair, bandwidth, pacing
- V verb study, debate, munch
- ADJ adjective purple, tall, ridiculous
- ADV adverb unfortunately, slowly
- P
preposition of, by, to
- PRO pronoun I, me, mine
- DET determiner the, a, that, those


## POS Tagging

- The process of assigning a part-of-speech or lexical class marker to each word in a collection.

WORD tag
the
koala
put
the
keys
on
the
table

## POS Tagging

- The process of assigning a part-of-speech or lexical class marker to each word in a collection.
word
tag
the
DET
koala
put
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the
table


## POS Tagging

- The process of assigning a part-of-speech or lexical class marker to each word in a collection.

WORD tag
the DET
koala $\mathbf{N}$
put
the
keys
on
the
table

## POS Tagging

- The process of assigning a part-of-speech or lexical class marker to each word in a collection.

WORD tag

| the | DET |
| :--- | :--- |
| koala | N |
| put | V |

the
keys
on
the
table

## POS Tagging

- The process of assigning a part-of-speech or lexical class marker to each word in a collection.

WORD tag

| the | DET |
| :--- | :--- |
| koala | N |
| put | V |
| the | DET |

keys
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| the | DET |
| keys | N |
| on | P |
| the | DET |

table

## POS Tagging

- The process of assigning a part-of-speech or lexical class marker to each word in a collection.

WORD tag

| the | DET |
| :--- | :--- |
| koala | $\mathbf{N}$ |
| put | V |
| the | DET |
| keys | N |
| on | P |
| the | DET |
| table | N |

## Why is POS Tagging Useful?

- First step of many practical tasks, e.g.
- Speech synthesis (aka text to speech)
- How to pronounce "lead"?
- OBject obJECT
- CONtent conTENT
- Parsing
- Need to know if a word is an N or V before you can parse
- Information extraction
- Finding names, relations, etc.
- Language modeling
- Backoff


## Why is POS Tagging Difficult?

- Words often have more than one POS: back
- The back door = adjective
- On my back =
- Win the voters back =
- Promised to back the bill =


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- Words often have more than one POS: back
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- On my back = noun
- Win the voters back = adverb
- Promised to back the bill =


## Why is POS Tagging Difficult?

- Words often have more than one POS: back
- The back door = adjective
- On my back = noun
- Win the voters back = adverb
- Promised to back the bill = verb
- The POS tagging problem is to determine the POS tag for a particular instance of a word.


## POS Tagging

- Input: Plays well with others
- Ambiguity: NNS/VBZ UH/JJ/NN/RB IN NNS
- Output: Plays/VBZ well/RB with/IN otr.Postags .JS


## POS tagging performance

- How many tags are correct? (Tag accuracy)
- About 97\% currently
- But baseline is already $90 \%$
- Baseline is performance of stupidest possible method
- Tag every word with its most frequent tag
- Tag unknown words as nouns
- Partly easy because
- Many words are unambiguous
- You get points for them (the, $a$, etc.) and for punctuation marks!


## Deciding on the correct part of speech can be difficult even for people

- Mrs/NNP Shaefer/NNP never/RB got/VBD around/RP to/TO joining/VBG
- All/DT we/PRP gotta/VBN do/VB is/VBZ go/VB around/IN the/DT corner/NN
- Chateau/NNP Petrus/NNP costs/VBZ around/RB 250/CD


## How difficult is POS tagging?

- About $11 \%$ of the word types in the Brown corpus are ambiguous with regard to part of speech
- But they tend to be very common words. E.g., that
- I know that he is honest = IN
- Yes, that play was nice = DT
- You can't go that far = RB
- $40 \%$ of the word tokens are ambiguous


## Review

- Backoff/Interpolation
- Parts of Speech
- What?
- Part of Speech Tagging
- What?
- Why?
- Easy or hard?
- Evaluation


## Open vs. Closed Classes

- Closed class: why?
- Determiners: a, an, the
- Prepositions: of, in, by, ...
- Auxiliaries: may, can, will had, been, ...
- Pronouns: I, you, she, mine, his, them, ...
- Usually function words (short common words which play a role in grammar)
- Open class: why?
- English has 4: Nouns, Verbs, Adjectives, Adverbs
- Many languages have these 4, but not all!


## Open vs. Closed Classes

- Closed class: a small fixed membership
- Determiners: a, an, the
- Prepositions: of, in, by, ...
- Auxiliaries: may, can, will had, been, ...
- Pronouns: I, you, she, mine, his, them, ...
- Usually function words (short common words which play a role in grammar)
- Open class: new ones can be created all the time
- English has 4: Nouns, Verbs, Adjectives, Adverbs
- Many languages have these 4, but not all!


## Open Class Words

- Nouns
- Proper nouns (Pittsburgh, Pat Gallagher)
- English capitalizes these.
- Common nouns (the rest).
- Count nouns and mass nouns
- Count: have plurals, get counted: goat/goats, one goat, two goats
- Mass: don't get counted (snow, salt, communism) (*two snows)
- Adverbs: tend to modify things
- Unfortunately, John walked home extremely slowly yesterday
- Directional/locative adverbs (here,home, downhill)
- Degree adverbs (extremely, very, somewhat)
- Manner adverbs (slowly, slinkily, delicately)
- Verbs
- In English, have morphological affixes (eat/eats/eaten)


## Closed Class Words

## Examples:

- prepositions: on, under, over, ...
- particles: up, down, on, off, ...
- determiners: a, an, the, ...
- pronouns: she, who, I, ..
- conjunctions: and, but, or, ...
- auxiliary verbs: can, may should, ...
- numerals: one, two, three, third, ...


## Prepositions from CELEX

| of | 540,085 | through | 14,964 | worth | 1,563 | pace | 12 |
| :--- | ---: | :--- | ---: | :--- | ---: | :--- | ---: |
| in | 331,235 | after | 13,670 | toward | 1,390 | nigh | 9 |
| for | 142,421 | between | 13,275 | plus | 750 | re | 4 |
| to | 125,691 | under | 9,525 | till | 686 | mid | 3 |
| with | 124,965 | per | 6,515 | amongst | 525 | o'er | 2 |
| on | 109,129 | among | 5,090 | via | 351 | but | 0 |
| at | 100,169 | within | 5,030 | amid | 222 | ere | 0 |
| by | 77,794 | towards | 4,700 | underneath | 164 | less | 0 |
| from | 74,843 | above | 3,056 | versus | 113 | midst | 0 |
| about | 38,428 | near | 2,026 | amidst | 67 | o | 0 |
| than | 20,210 | off | 1,695 | sans | 20 | thru | 0 |
| over | 18,071 | past | 1,575 | circa | 14 | vice | 0 |

## POS Tagging Choosing a Tagset

- There are so many parts of speech, potential distinctions we can draw
- To do POS tagging, we need to choose a standard set of tags to work with
- Could pick very coarse tagsets
- N, V, Adj, Adv.
- More commonly used set is finer grained, the "Penn TreeBank tagset", 45 tags
- Even more fine-grained tagsets exist


## Penn TreeBank POS Tagset

| Tag | Description | Example | Tag | Description | Example |
| :---: | :---: | :---: | :---: | :---: | :---: |
| CC | coordin. conjunction | and, but, or | SYM | symbol | $+, \%, \&$ |
| CD | cardinal number | one, two, three | TO | "to" | to |
| DT | determiner | $a$, the | UH | interjection | ah, oops |
| EX | existential 'there' | there | VB | verb, base form | eat |
| FW | foreign word | mea culpa | VBD | verb, past tense | ate |
| IN | preposition/sub-conj | of, in, by | VBG | verb, gerund | eating |
| JJ | adjective | yellow | VBN | verb, past participle | eaten |
| JJR | adj., comparative | bigger | VBP | verb, non-3sg pres | eat |
| JJS | adj., superlative | wildest | VBZ | verb, 3 sg pres | eats |
| LS | list item marker | 1,2, One | WDT | wh-determiner | which, that |
| MD | modal | can, should | WP | wh-pronoun | what, who |
| NN | noun, sing. or mass | llama | WPS | possessive wh- | whose |
| NNS | noun, plural | llamas | WRB | wh-adverb | how, where |
| NNP | proper noun, singular | IBM | \$ | dollar sign | \$ |
| NNPS | proper noun, plural | Carolinas | \# | pound sign | \# |
| PDT | predeterminer | all, both | " | left quote | 'or ${ }^{\prime}$ |
| POS | possessive ending | 's | " | right quote | , or " |
| PRP | personal pronoun | I, you, he | ( | left parenthesis | [, (, \{, < |
| PRP\$ | possessive pronoun | your, one's | ) | right parenthesis | ], ), \}, > |
| RB | adverb | quickly, never | , | comma |  |
| RBR | adverb, comparative | faster | . | sentence-final punc | ! ? |
| RBS | adverb, superlative | fastest | : | mid-sentence punc | : ; ... -- |
| RP | particle | up, off |  |  |  |

## Using the Penn Tagset

- The/? grand/? jury/? commmented/? on/? a/? number/? of/? other/? topics/? ./?


## Using the Penn Tagset

- The/DT grand/JJ jury/NN commented/VBD on/IN a/DT number/NN of/IN other/JJ topics/NNS ./.


## Recall POS Tagging Difficulty

- Words often have more than one POS: back
- The back door = JJ
- On my back = NN
- Win the voters back = RB
- Promised to back the bill = VB
- The POS tagging problem is to determine the POS tag for a particular instance of a word.


## How Hard is POS Tagging? Measuring Ambiguity

|  | 87-tag Original Brown | 45-tag Treebank Brown |
| :---: | :---: | :---: |
| Unambiguous (1 tag) | $\mathbf{4 4 , 0 1 9}$ | $\mathbf{3 8 , 8 5 7}$ |
| Ambiguous (2-7 tags) | $\mathbf{5 , 4 9 0}$ | $\mathbf{8 8 4 4}$ |
| Details: | 2 tags | 4,967 |
| 6,731 |  |  |
| 3 tags | 411 | 1621 |
| 4 tags | 91 | 357 |
| 5 tags | 17 | 90 |
| 6 tags | 2 (well, beat) | 32 |
| 7 tags | 2 (still, down) | 6 (well, set, round, |
|  |  | 4 open, fit, down) |
| 8 tags |  | 3 (s, half, back, a) |
| 9 tags |  |  |
|  |  |  |

## Tagging Whole Sentences with POS is Hard too

- Ambiguous POS contexts
- E.g., Time flies like an arrow.
- Possible POS assignments
- Time/[V,N] flies/[V,N] like/[V,Prep] an/Det arrow/N
- Time/N flies/V like/Prep an/Det arrow/N
- Time/V flies/N like/Prep an/Det arrow/N
- Time/N flies/N like/V an/Det arrow/N
- .....


## How Do We Disambiguate POS?

- Many words have only one POS tag (e.g. is, Mary, smallest)
- Others have a single most likely tag (e.g. Dog is less used as a V)
- Tags also tend to co-occur regularly with other tags (e.g. Det, N)
- In addition to conditional probabilities of words $\mathrm{P}\left(\mathrm{w}_{1} \mid \mathrm{w}_{\mathrm{n}-1}\right)$, we can look at POS likelihoods $\mathrm{P}\left(\mathrm{t}_{1} \mid \mathrm{t}_{\mathrm{n}-1}\right)$ to disambiguate sentences and to assess sentence likelihoods


## More and Better Features Feature-based tagger

- Can do surprisingly well just looking at a word by itself:
- Word the: the $\rightarrow$ DT
- Lowercased word Importantly: importantly $\rightarrow$ RB
- Prefixes unfathomable: un- $\rightarrow$ JJ
- Suffixes Importantly: -ly $\rightarrow$ RB
- Capitalization Meridian: CAP $\rightarrow$ NNP
- Word shapes 35 -year: $\mathrm{d}-\mathrm{x} \rightarrow \mathrm{JJ}$


## Overview: POS Tagging Accuracies

- Most freq tag:
- Trigram HMM:
~95\% / ~55\%
- Maxent P(t|w):
93.7\% / 82.6\%
- Upper bound:
~98\% (human)


## Rule-Based Tagging

- Start with a dictionary
- Assign all possible tags to words from the dictionary
- Write rules by hand to selectively remove tags
- Leaving the correct tag for each word.


## Start With a Dictionary

- she:
- promised:
- to
- back:
- the:
- bill:


## Start With a Dictionary

- she:

PRP

- promised: VBN,VBD
- to

TO

- back:
- the:

VB, JJ, RB, NN

- bill:

DT
NN, VB

## Assign Every Possible Tag

|  | NN |  |  |
| :---: | :--- | :--- | :--- |
|  | RB |  |  |
| VBN | JJ | VB |  |
| PRP VBD | TO | VB | DT |
| She promised to | lack the bill |  |  |

## Write Rules to Eliminate Tags

Eliminate VBN if VBD is an option when VBN|VBD follows "<start> PRP"

NN
RB

VBN
PRP VBD
She promised

JJ VB
TO VB DT NN
to back the bill

## POS tag sequences

- Some tag sequences are more likely occur than others
- POS Ngram view
https://books.google.com/ngrams/graph?c ontent $=$ ADJ + NOUN \%2C ADV + NO UN \%2C+ ADV + VERB

> Existing methods often model POS tagging as a sequence tagging problem

## POS Tagging as Sequence Classification

- We are given a sentence (an "observation" or "sequence of observations")
- Secretariat is expected to race tomorrow
- What is the best sequence of tags that corresponds to this sequence of observations?
- Probabilistic view:
- Consider all possible sequences of tags
- Out of this universe of sequences, choose the tag sequence which is most probable given the observation sequence of $n$ words $\mathrm{w}_{1} \ldots \mathrm{w}_{\mathrm{n}}$.


## How do you predict the tags?

- Two types of information are useful
- Relations between words and tags
- Relations between tags and tags
- DT NN, DT JJ NN...


## Getting to HMMs (Hidden Markov Models)

- We want, out of all sequences of $n$ tags $t_{1} \ldots t_{n}$ the single tag sequence such that $\mathrm{P}\left(\mathrm{t}_{1} \ldots \mathrm{t}_{n} \mid \mathrm{w}_{1} \ldots \mathrm{w}_{\mathrm{n}}\right)$ is highest.

$$
\hat{t}_{1}^{n}=\underset{t_{1}^{n}}{\operatorname{argmax}} P\left(t_{1}^{n} \mid w_{1}^{n}\right)
$$

- Hat ^ means "our estimate of the best one"
- $\operatorname{Argmax}_{x} f(x)$ means "the $x$ such that $f(x)$ is maximized"


## Getting to HMMs

- This equation is guaranteed to give us the best tag sequence

$$
\hat{\tau}_{1}^{n}=\underset{t_{1}^{n}}{\operatorname{argmax}} P\left(t_{1}^{n} \mid w_{1}^{n}\right)
$$

- But how to make it operational? How to compute this value?
- Intuition of Bayesian classification:
- Use Bayes rule to transform this equation into a set of other probabilities that are easier to compute


## Using Bayes Rule

$$
\begin{gathered}
P(x \mid y)=\frac{P(y \mid x) P(x)}{P(y)} \\
\hat{t}_{1}^{n}=\underset{t_{1}^{n}}{\operatorname{argmax}} \frac{P\left(w_{1}^{n} \mid t_{1}^{n}\right) P\left(t_{1}^{n}\right)}{P\left(w_{1}^{n}\right)} \\
\hat{t}_{1}^{n}=\underset{t_{1}^{n}}{\operatorname{argmax}} P\left(w_{1}^{n} \mid t_{1}^{n}\right) P\left(t_{1}^{n}\right)
\end{gathered}
$$

## Statistical POS tagging

- What is the most likely sequence of tags for the given sequence of words w

$$
\begin{aligned}
\underset{\mathbf{t}}{\operatorname{argmax}} P(\mathbf{t} \mid \mathbf{w}) & =\underset{\mathbf{t}}{\operatorname{argmax}} \frac{P(\mathbf{t}, \mathbf{w})}{P(\mathbf{w})} \\
& =\underset{\mathbf{t}}{\operatorname{argmax}} P(\mathbf{t}, \mathbf{w}) \\
& =\underset{\mathbf{t}}{\operatorname{argmax}} P(\mathbf{t}) P(\mathbf{w} \mid \mathbf{t})
\end{aligned}
$$

P( DT JJ NN | a smart dog) =

## Statistical POS tagging

- What is the most likely sequence of tags for the given sequence of words w

$$
\begin{aligned}
\underset{\mathbf{t}}{\operatorname{argmax}} P(\mathbf{t} \mid \mathbf{w}) & =\underset{\mathbf{t}}{\operatorname{argmax}} \frac{P(\mathbf{t}, \mathbf{w})}{P(\mathbf{w})} \\
& =\underset{\mathbf{t}}{\operatorname{argmax}} P(\mathbf{t}, \mathbf{w}) \\
& =\underset{\mathbf{t}}{\operatorname{argmax}} P(\mathbf{t}) P(\mathbf{w} \mid \mathbf{t})
\end{aligned}
$$

$$
\begin{aligned}
\mathrm{P}(\mathrm{DT} \text { JJ NN | a smart dog) }) & \mathrm{P}(\text { (DD JJ NN a smart dog) / P (a smart dog) } \\
& \propto \mathrm{P}(D D \mathrm{JJ} N N \text { a smart dog) } \\
& =\mathrm{P}(\text { (DD JJ NN) P(a smart dog | DD JJ NN })
\end{aligned}
$$

## Likelihood and Prior

$$
\begin{aligned}
& \text { Q. } \hat{t}_{1}^{n}=\underset{t_{1}^{n}}{\operatorname{argmax}} \overbrace{P\left(w_{1}^{n} \mid t_{1}^{n}\right)}^{\text {likelihood }} \overbrace{P\left(t_{1}^{n}\right)}^{\text {prior }} \\
& P\left(w_{1}^{n} \mid t_{1}^{n}\right) \approx \prod_{i=1} P\left(w_{i} \mid t_{i}\right) \\
& P\left(t_{1}^{n}\right) \approx \prod_{i=1}^{n} P\left(t_{i} \mid t_{i-1}\right) \\
& \text { ( }{ }_{t_{1}^{n}}^{\operatorname{argmax}} P\left(t_{1}^{n} \mid w_{1}^{n}\right) \approx \underset{t_{1}^{n}}{\operatorname{argmax}} \prod_{i=1}^{n} P\left(w_{i} \mid t_{i}\right) P\left(t_{i} \mid t_{i-1}\right)
\end{aligned}
$$

## Two Kinds of Probabilities

- Tag transition probabilities $p\left(\mathrm{t}_{\mathrm{i}} \mathrm{t}_{\mathrm{i}-1}\right)$
- Determiners likely to precede adjs and nouns
- That/DT flight/NN
- The/DT yellow/JJ hat/NN
- So we expect P(NN|DT) and P(JJ|DT) to be high
- But P(DT|JJ) to be:
- Compute P(NN|DT) by counting in a labeled

$$
\text { corpus: } \quad P\left(t_{i} \mid t_{i-1}\right)=\frac{C\left(t_{i-1}, t_{i}\right)}{C\left(t_{i-1}\right)}
$$

$$
P(N N \mid D T)=\frac{C(D T, N N)}{C(D T)}=\frac{56,509}{116,454}=.49
$$

## Two Kinds of Probabilities

- Word likelihood (emission) probabilities $\mathrm{p}\left(\mathrm{w}_{\mathrm{i}} \mid \mathrm{t}_{\mathrm{i}}\right)$
- VBZ (3sg Pres verb) likely to be "is"
- Compute P(is $\mid$ VBZ ) by counting in a labeled

$$
\begin{aligned}
& \text { corpus: } P\left(w_{i} \mid t_{i}\right)=\frac{C\left(t_{i}, w_{i}\right)}{C\left(t_{i}\right)} \\
& P(i s \mid V B Z)=\frac{C(V B Z, i s)}{C(V B Z)}=\frac{10,073}{21,627}=.47
\end{aligned}
$$

## Put them together

- Two independent assumptions
- Approximate $\mathrm{P}(\mathbf{t})$ by a bi(or N$)$-gram model
- Assume each word depends only on its POS tag



## Table representation

Transition Matrix $A$

|  | $\mathbf{D}$ | $\mathbf{N}$ | $\mathbf{V}$ | $\mathbf{A}$ | $\cdot$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{D}$ |  | 0.8 |  | 0.2 |  |
| $\mathbf{N}$ |  | 0.7 | 0.3 |  |  |
| $\mathbf{V}$ | 0.6 |  |  |  | 0.4 |
| $\mathbf{A}$ |  | 0.8 |  | 0.2 |  |
| . |  |  |  |  |  |

Initial state vector $\pi$

|  | $\mathbf{D}$ | $\mathbf{N}$ | $\mathbf{V}$ | $\mathbf{A}$ | . |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\pi$ | 1.0 |  |  |  |  |

Emission Matrix $B$

|  | the | man | ball | throws | sees | red | blue | . |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| D | 1.0 |  |  |  |  |  |  |  |
| N |  | 0.7 | 0.3 |  |  |  |  |  |
| V |  |  |  | 0.6 | 0.4 |  |  |  |
| A |  |  |  |  |  | 0.8 | 0.2 |  |
| . |  |  |  |  |  |  |  | 1 |



Let $\lambda=\{A, B, \pi\}$ represents all paramete

## Prediction in generative model

- Inference: What is the most likely sequence of tags for the given sequence of words $\mathbf{w}$

- What are the latent states that most likely generate the sequence of word $\mathbf{w}$


## Example: The Verb "race"

- Secretariat/NNP is/VBZ expected/VBN to/TO race/VB tomorrow/NR
- People/NNS continue/VB to/TO inquire/VB the/DT reason/NN for/IN the/DT race/NN for/IN outer/JJ space/NN
- How do we pick the right tag?


## Disambiguating "race"

(a)

(b)


## Example

- $\mathrm{P}(\mathrm{NN} \mid \mathrm{TO})=.00047$
- $P($ VB|TO $)=.83$
- $P($ race|NN $)=.00057$
- $P($ race $\mid V B)=.00012$
- $P(N R \mid V B)=.0027$
- $P(N R \mid N N)=.0012$
- $P(V B \mid T O) P(N R \mid V B) P($ race $\mid V B)=.00000027$
- $P(N N \mid T O) P(N R \mid N N) P($ race $\mid N N)=.00000000032$
- So we (correctly) choose the verb reading


## Hidden Markov Models

- What we've described with these two kinds of probabilities is a Hidden Markov Model (HMM)


## Definitions

- A weighted finite-state automaton adds probabilities to the arcs
- The sum of the probabilities leaving any arc must sum to one
- A Markov chain is a special case of a WFSA in which the input sequence uniquely determines which states the automaton will go through
- Markov chains can't represent inherently ambiguous problems
- Useful for assigning probabilities to unambiguous sequences


## Markov Chain for Weather



## Weather continued



## Markov Chain for Words



## Markov Chain: "First-order observable Markov Model"

- A set of states
- $\mathrm{Q}=\mathrm{q}_{1}, \mathrm{q}_{2} . . \mathrm{q}_{\mathrm{N}}$, the state at time t is $\mathrm{q}_{\mathrm{t}}$
- Transition probabilities:
- a set of probabilities $A=a_{01} a_{02} \ldots a_{n 1} \ldots a_{n n}$.
- Each $\mathrm{a}_{\mathrm{ij}}$ represents the probability of transitioning from state $i$ to state $j$
- The set of these is the transition probability matrix A
- Current state only depends on previous state

$$
P\left(q_{i} \mid q_{1} \ldots q_{i-1}\right)=P\left(q_{i} \mid q_{i-1}\right)
$$

## Markov Chain for Weather

- What is the probability of 4 consecutive rainy days?
- Sequence is rainy-rainy-rainy-rainy
- I.e., state sequence is 3-3-3-3
- $P(3,3,3,3)=$


## Markov Chain for Weather

- What is the probability of 4 consecutive rainy days?
- Sequence is rainy-rainy-rainy-rainy
- I.e., state sequence is 3-3-3-3
- $P(3,3,3,3)=$
- $\pi_{3} \mathrm{a}_{33} \mathrm{a}_{33} \mathrm{a}_{33}=0.2 \times(0.6)^{3}=0.0432$


## Review

- Tagsets
- What?
- Example(s)
- Baseline(s) for tagging evaluation
- Two types of probabilities for POS tagging - assumptions
- Markov Chain vs Hidden Markov Model


## HMM for Ice Cream

- You are a climatologist in the year 2799
- Studying global warming
- You can't find any records of the weather in Pittsburgh for summer of 2018
- But you find a diary
- Which lists how many ice-creams someone ate every date that summer
- Our job: figure out how hot it was


## Hidden Markov Model

- For Markov chains, the output symbols are the same as the states.
- See hot weather: we're in state hot
- But in part-of-speech tagging (and other things)
- The output symbols are words
- But the hidden states are part-of-speech tags
- So we need an extension!
- A Hidden Markov Model is an extension of a Markov chain in which the input symbols are not the same as the states.
- This means we don't know which state we are in.


## Hidden Markov Models

- States $\mathrm{Q}=\mathrm{q}_{1}, \mathrm{q}_{2} \ldots \mathrm{q}_{\mathrm{N}}$;
- Observations $\mathrm{O}=\mathrm{o}_{1}, \mathrm{o}_{2} \ldots \mathrm{o}_{\mathrm{N}}$;
- Each observation is a symbol from a vocabulary V $=\left\{\mathrm{v}_{1}, \mathrm{v}_{2}, \ldots \mathrm{v}_{\mathrm{v}}\right\}$
- Transition probabilities
- Transition probability matrix $\mathrm{A}=\left\{\mathrm{a}_{\mathrm{ij}}\right\}$

$$
a_{i j}=P\left(q_{t}=j \mid q_{t-1}=i\right) \quad 1 \leq i, j \leq N
$$

- Observation likelihoods
- Output probability matrix $B=\left\{b_{i}(\mathrm{k})\right\}$

$$
\begin{aligned}
& b_{i}(k)=P\left(X_{t}=o_{k} \mid q_{t}=i\right) \\
& \pi_{i}=P\left(q_{1}=i\right) \quad 1 \leq i \leq N
\end{aligned}
$$

- Special initial probability vector $\pi$


## Task

- Given
- Ice Cream Observation Sequence: 1,2,3,2,2,2,3...
- Produce:
- Weather Sequence: H,C,H,H,H,C...


## Weather/ I ce Cream HMM

- Hidden States:
- Transition probabilities:
- Observations:


## Weather/ I ce Cream HMM

- Hidden States: \{Hot,Cold\}
- Transition probabilities (A Matrix) between H and C
- Observations: $\{1,2,3\}$ \# of ice creams eaten per day


## HMM for I ce Cream



## Back to POS Tagging: Transition Probabilities



## Observation Likelihoods



## What can HMMs Do?

- Likelihood: Given an HMM $\lambda$ and an observation sequence 0 , determine the likelihood $\mathrm{P}(\mathrm{O}, \lambda)$ : language modeling
- Decoding: Given an observation sequence O and an $\mathrm{HMM} \lambda$, discover the best hidden state sequence Q: Given seq of ice creams, what was the most likely weather on those days? (tagging)
- Learning: Given an observation sequence O and the set of states in the HMM, learn the HMM parameters


## Decoding

- Ok, now we have a complete model that can give us what we need. Recall that we need to get

$$
\hat{t}_{1}^{n}=\underset{t_{1}^{n}}{\operatorname{argmax}} P\left(t_{1}^{n} \mid w_{1}^{n}\right)
$$

- We could just enumerate all paths given the input and use the model to assign probabilities to each.
- Not a good idea.
- In practice: Viterbi Algorithm (dynamic programming)


## Viterbi Algorithm

- Intuition: since state transition out of a state only depend on the current state (and not previous states), we can record for each state the optimal path
- We record
- Cheapest cost to state at step
- Backtrace for that state to best predecessor


## Viterbi Summary

- Create an array
- With columns corresponding to inputs
- Rows corresponding to possible states
- Sweep through the array in one pass filling the columns left to right using our transition probs and observations probs
- Dynamic programming key is that we need only store the MAX prob path to each cell (not all paths).



## Another Viterbi Example

- Analyzing "Fish sleep"
- Done in class


## Evaluation

- So once you have your POS tagger running how do you evaluate it?
- Overall error rate with respect to a goldstandard test set.
- Error rates on particular tags
- Error rates on particular words
- Tag confusions...
- Need a baseline - just the most frequent tag is $90 \%$ accurate!


## Error Analysis

- Look at a confusion matrix

|  | IN | JJ | NN | NNP | RB | VBD | VBN |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| IN | - | .2 |  |  | .7 |  |  |
| JJ | .2 | - | $\mathbf{3 . 3}$ | 2.1 | 1.7 | .2 | $\mathbf{2 . 7}$ |
| NN |  | $\mathbf{8 . 7}$ | - |  |  |  | .2 |
| NNP | .2 | $\mathbf{3 . 3}$ | $\mathbf{4 . 1}$ | - | .2 |  |  |
| RB | $\mathbf{2 . 2}$ | 2.0 | .5 |  | - |  |  |
| VBD |  | .3 | .5 |  |  | - | $\mathbf{4 . 4}$ |
| VBN |  | $\mathbf{2 . 8}$ |  |  |  | $\mathbf{2 . 6}$ | - |

- See what errors are causing problems
- Noun (NN) vs ProperNoun (NNP) vs Adj (JJ)
- Preterite (VBD) vs Participle (VBN) vs Adjective (JJ)


## Evaluation

- The result is compared with a manually coded "Gold Standard"
- Typically accuracy reaches 96-97\%
- This may be compared with result for a baseline tagger (one that uses no context).
- Important: $100 \%$ is impossible even for human annotators.


## More Complex I ssues

- Tag indeterminacy: when 'truth' isn't clear Caribbean cooking, child seat
- Tagging multipart words wouldn't --> would/MD n't/RB
- How to handle unknown words
- Assume all tags equally likely
- Assume same tag distribution as all other singletons in corpus
- Use morphology, word length,....


## Other Tagging Tasks

- Noun Phrase (NP) Chunking
- [the student] said [the exam] is hard
- Three tabs
- B = beginning of NP
- I = continuing in NP
- $\mathrm{O}=$ other word
- Tagging result
- The/B student/I said/O the/B exam/I is/0 hard/0


## Summary

- Parts of speech
- Tagsets
- Part of speech tagging
- Rule-Based, HMM Tagging
- Other methods later in course

