Suppose we have the following PCFG for modeling some simple English sentences.

- Terminals \{the, a, some, steak, fork, sauce, Alice, golden, hot, ate, I ...\}
- Non-terminals \{S, NP, VP, PP, NBAR, NN, PRPN, PRON, P, JJ, VB $\}$

| 1.0 S $\rightarrow$ NP VP | $\begin{aligned} & 0.6 \mathrm{VP} \rightarrow \mathrm{VB} \mathrm{NP} \\ & 0.3 \mathrm{VP} \rightarrow \mathrm{VB} \\ & 0.1 \mathrm{VP} \rightarrow \mathrm{VP} \mathrm{PP} \end{aligned}$ | $1.0 \mathrm{PP} \rightarrow \mathrm{P} \mathrm{NP}$ |
| :---: | :---: | :---: |
|  |  | $1.0 \mathrm{PRON} \rightarrow \mathrm{I}$ |
| $\begin{aligned} & 0.5 \mathrm{NP} \rightarrow \text { DT NBAR } \\ & 0.3 \mathrm{NP} \rightarrow \text { PRPN } \\ & 0.2 \mathrm{NP} \rightarrow \text { PRON } \end{aligned}$ | $\begin{aligned} & 0.75 \text { NBAR } \rightarrow \text { NN } \\ & 0.15 \text { NBAR } \rightarrow \text { NBAR PP } \\ & 0.1 \text { NBAR } \rightarrow \text { JJ NBAR } \end{aligned}$ | 1.0 PRPN $\rightarrow$ Alice |
|  |  | $\begin{aligned} & 0.5 \mathrm{JJ} \rightarrow \text { golden } \\ & 0.5 \mathrm{JJ} \rightarrow \text { hot } \end{aligned}$ |
| $\begin{aligned} & 0.4 \mathrm{DT} \rightarrow \text { the } \\ & 0.4 \mathrm{DT} \rightarrow \text { a } \\ & 0.2 \mathrm{DT} \rightarrow \text { some } \end{aligned}$ | $0.35 \mathrm{NN} \rightarrow$ steak <br> $0.35 \mathrm{NN} \rightarrow$ sauce <br> 0.3 $\mathrm{NN} \rightarrow$ fork | $1.0 \mathrm{VB} \rightarrow$ ate |
|  |  | $1.0 \mathrm{P} \rightarrow$ with |

1. What is the probability of the sentence "I ate" in the grammar?
2. What would be the probability of the sentence if it had a second parse?
